

Modeling and Learning Semantic Co-Compositionality through Prototype Projections and Neural Networks

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Two contributions in our work

New model of
compositionality
in word vector space

Unsupervised word vector
re-training algorithm
considering compositionality

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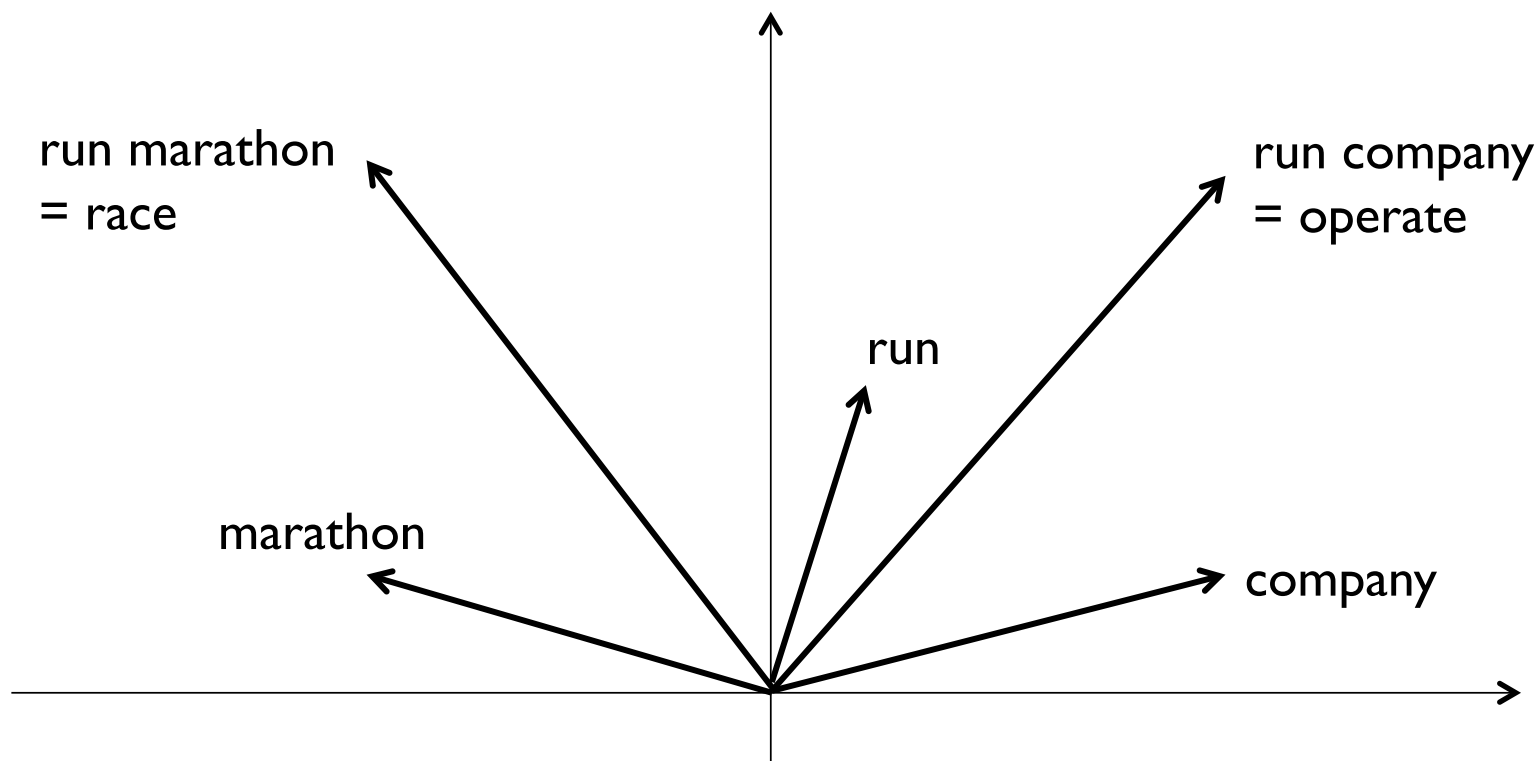
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Modeling of compositionality in word vector space

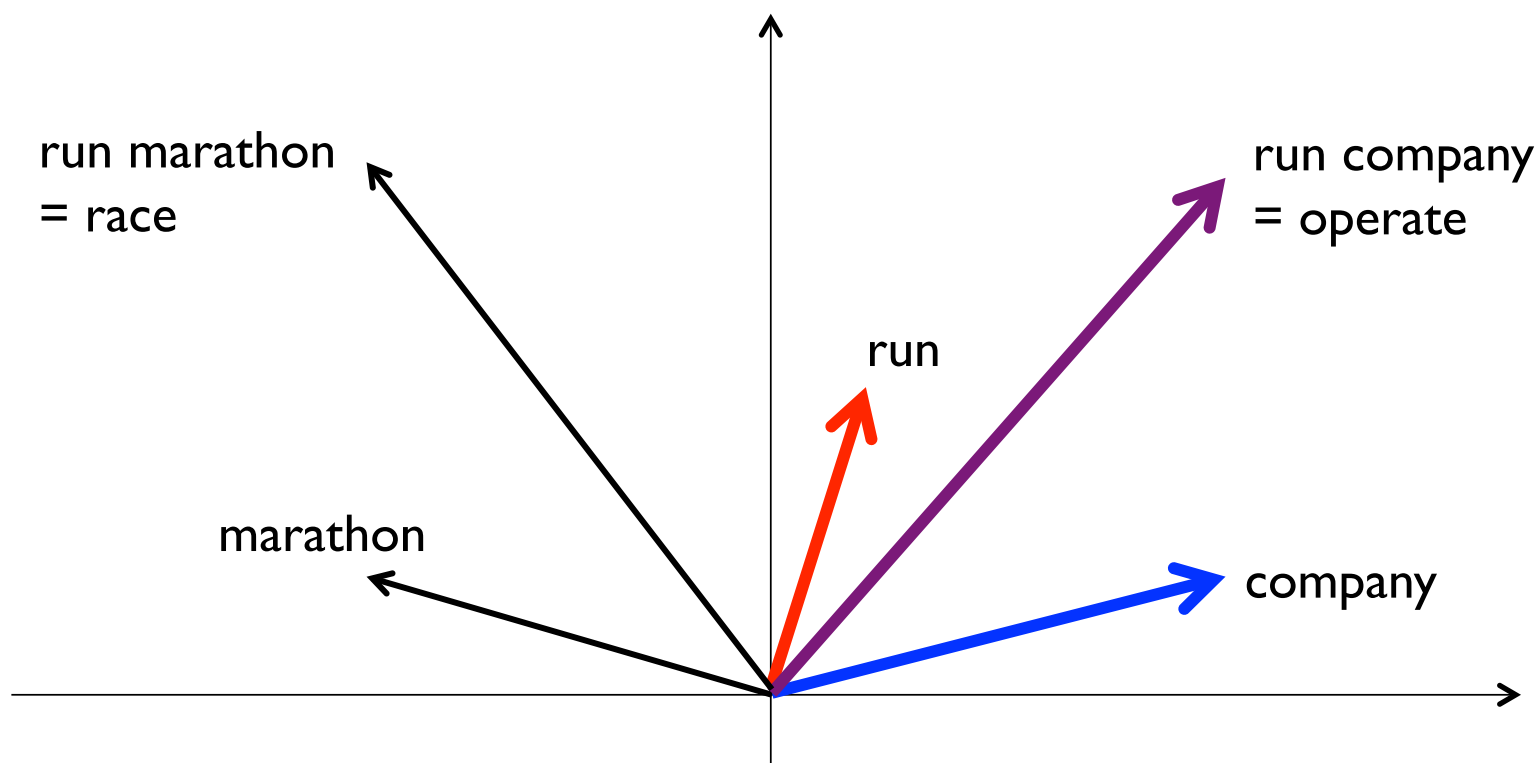
From word to **phrase representation** with matrix-vector operation

[Mitchell and Lapata 08], [Baroni and Zamparell 10], [Socher+ 12], [Van de Cruys+ 13]



Modeling of compositionality in word vector space

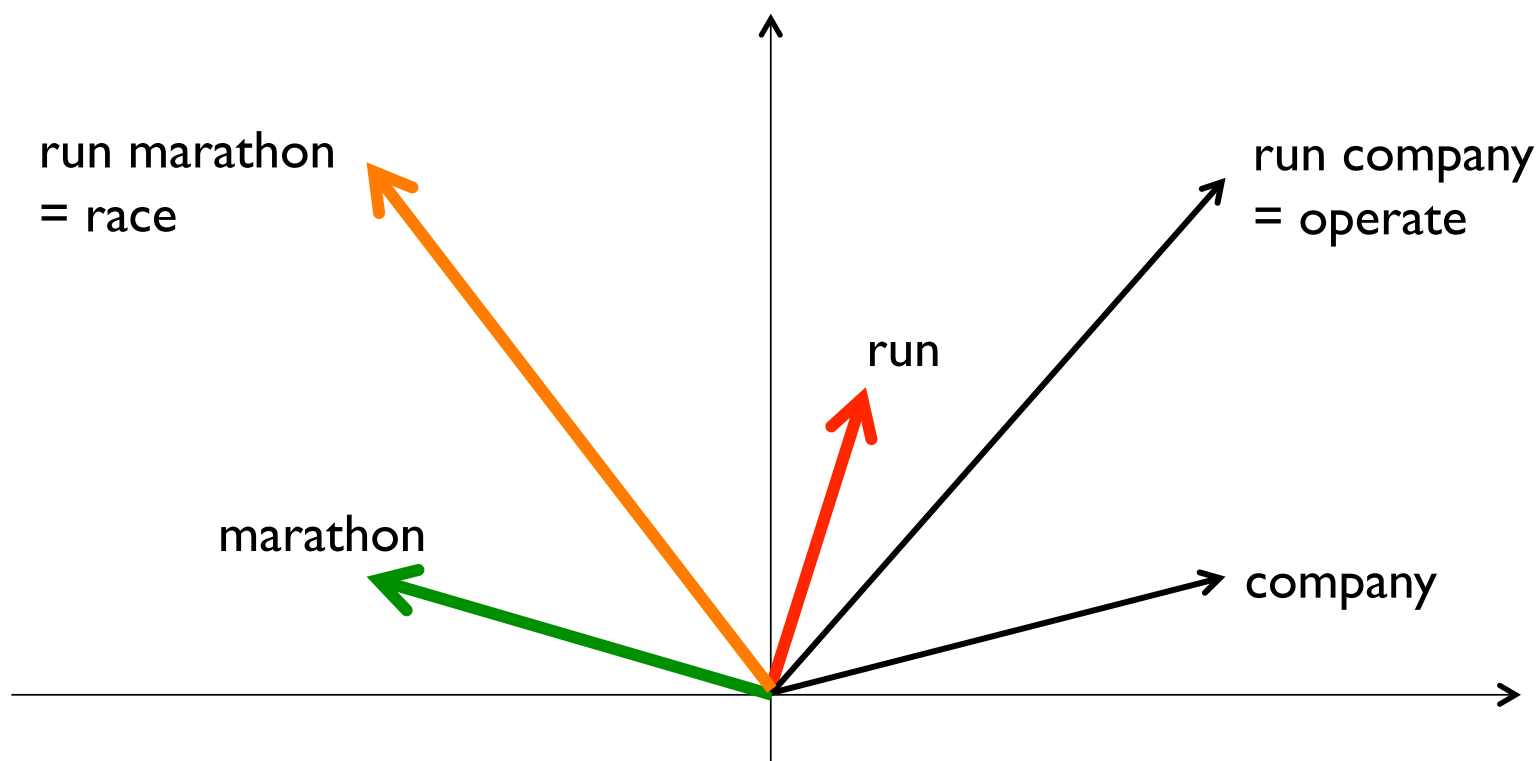
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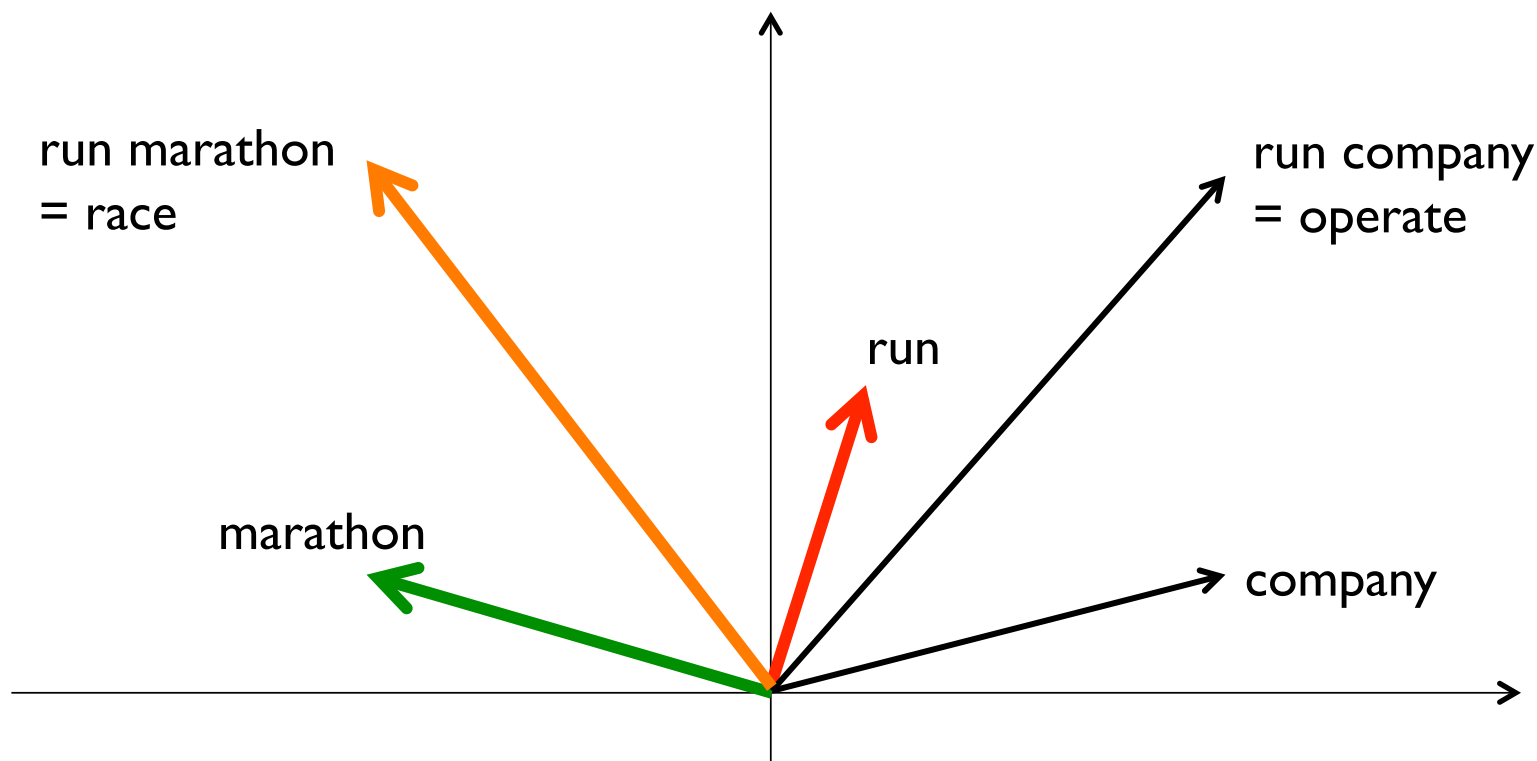
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Modeling of compositionality in word vector space

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New model inspired by **Co-Compositionality**

Main Idea : Co-Compositionality [Pustejovsky 1995]

Co-compositionality

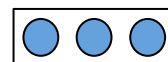
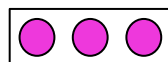
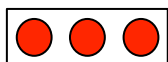
Verb and object are allowed to **modify each other's meanings** and generate the overall semantics

Main Idea : Co-Compositionality [Pustejovsky 1995]

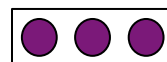
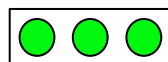
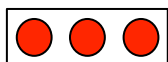
Co-compositionality

Verb and object are allowed to **modify each other's meanings** and generate the overall semantics

f(run , company) = operate



f(run , marathon) = race

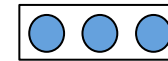
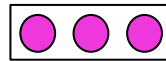
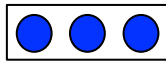


Main Idea : Co-Compositionality [Pustejovsky 1995]

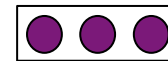
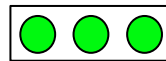
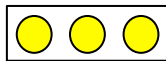
Co-compositionality

Verb and object are allowed to **modify each other's meanings** and generate the overall semantics

$f(\text{run}_{\text{company}}, \text{company}) = \text{operate}$



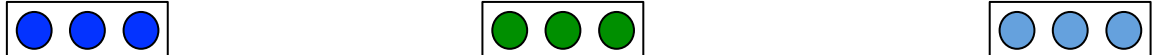
$f(\text{run}_{\text{marathon}}, \text{marathon}) = \text{race}$



Main Idea : Co-Compositionality [Pustejovsky 1995]

Co-compositionality

Verb and object are allowed to **modify each other's meanings** and generate the overall semantics

$$f(\text{run}_{\text{company}}, \text{company}_{\text{run}}) = \text{operate}$$


The diagram illustrates the composition of the verb 'run' and the object 'company' to form the overall meaning 'operate'. Each word is represented by a horizontal box containing three colored circles. 'run' is represented by three blue circles, 'company' by three green circles, and 'operate' by three light blue circles.

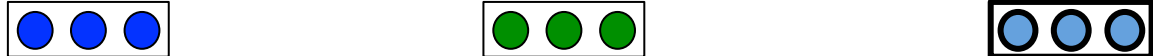
$$f(\text{run}_{\text{marathon}}, \text{marathon}_{\text{run}}) = \text{race}$$


The diagram illustrates the composition of the verb 'run' and the object 'marathon' to form the overall meaning 'race'. Each word is represented by a horizontal box containing three colored circles. 'run' is represented by three yellow circles, 'marathon' by three orange circles, and 'race' by three purple circles.

Main Idea : Co-Compositionality [Pustejovsky 1995]

Co-compositionality

Verb and object are allowed to **modify each other's meanings** and generate the overall semantics

$$f(\text{run}_{\text{company}}, \text{company}_{\text{run}}) = \mathbf{operate}$$


The diagram illustrates the composition of 'run' and 'company' into 'operate'. Below 'run' are three blue circles in a box. Below 'company' are three green circles in a box. Below 'operate' are three light blue circles in a box.

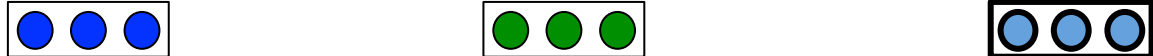
$$f(\text{run}_{\text{marathon}}, \text{marathon}_{\text{run}}) = \mathbf{race}$$


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Co-compositionality

Verb and object are allowed to **modify each other's meanings** and generate the overall semantics

$$f(\text{run}_{\text{company}}, \text{company}_{\text{run}}) = \text{operate}$$


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Question

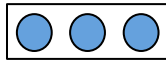
How do we implement co-compositionality in vector space ?

Prototype Projection

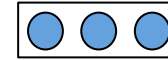
**Matrix-vector operation as an
implementation for Co-Compositionality**

Co-Compositionality with Prototype Projections

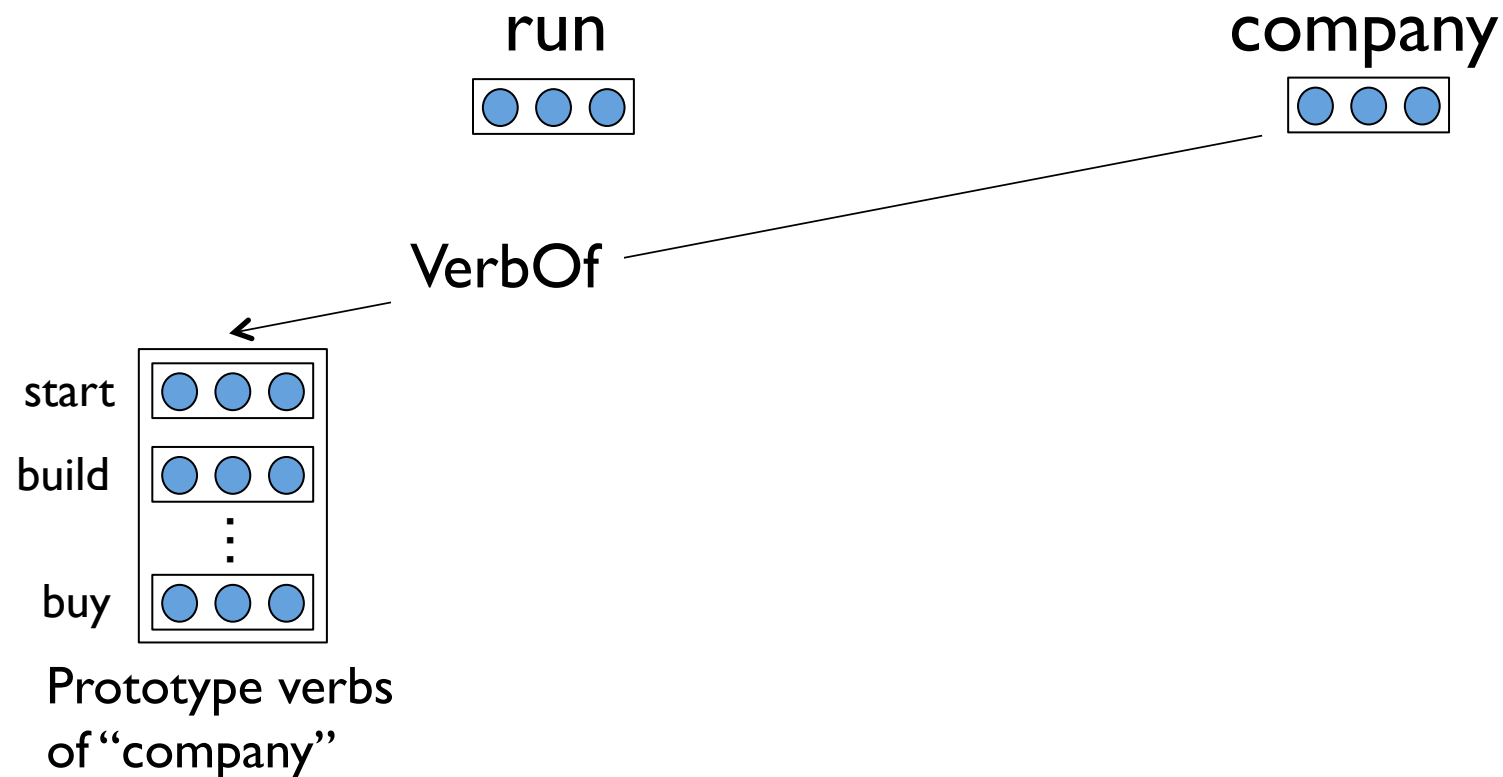
run



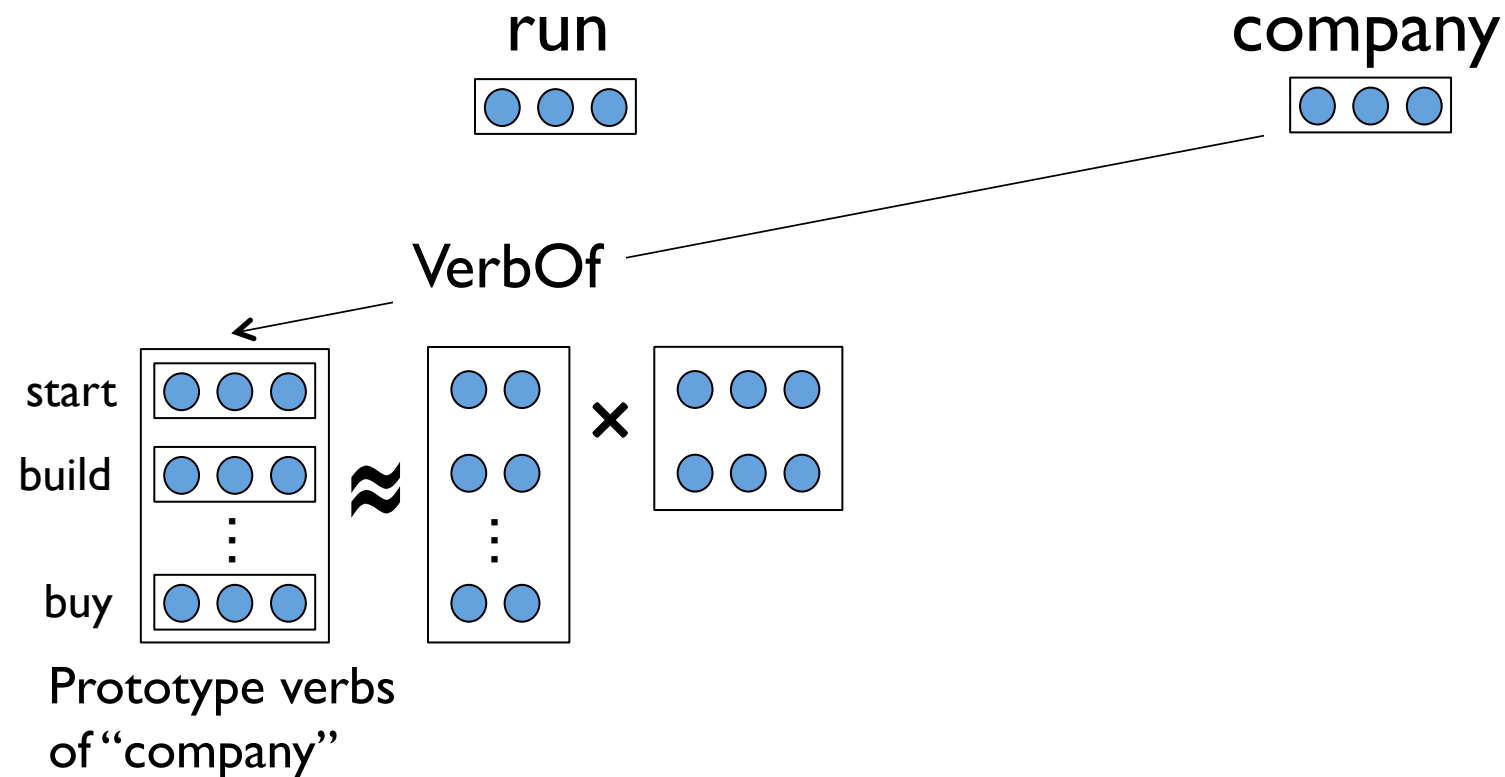
company



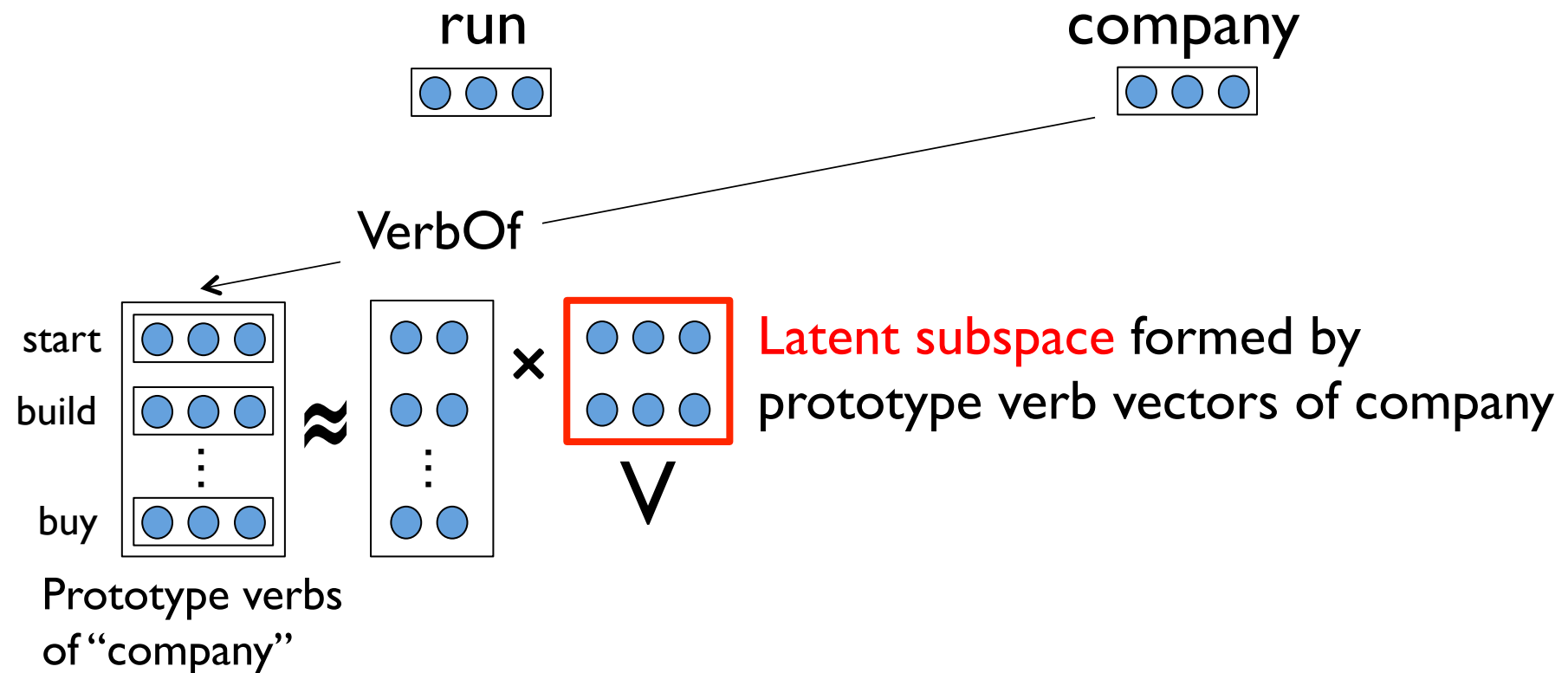
Co-Compositionality with Prototype Projections



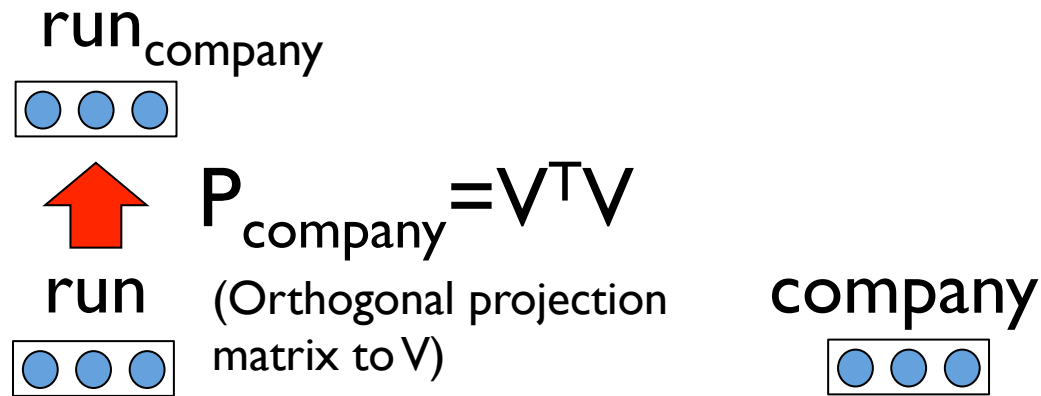
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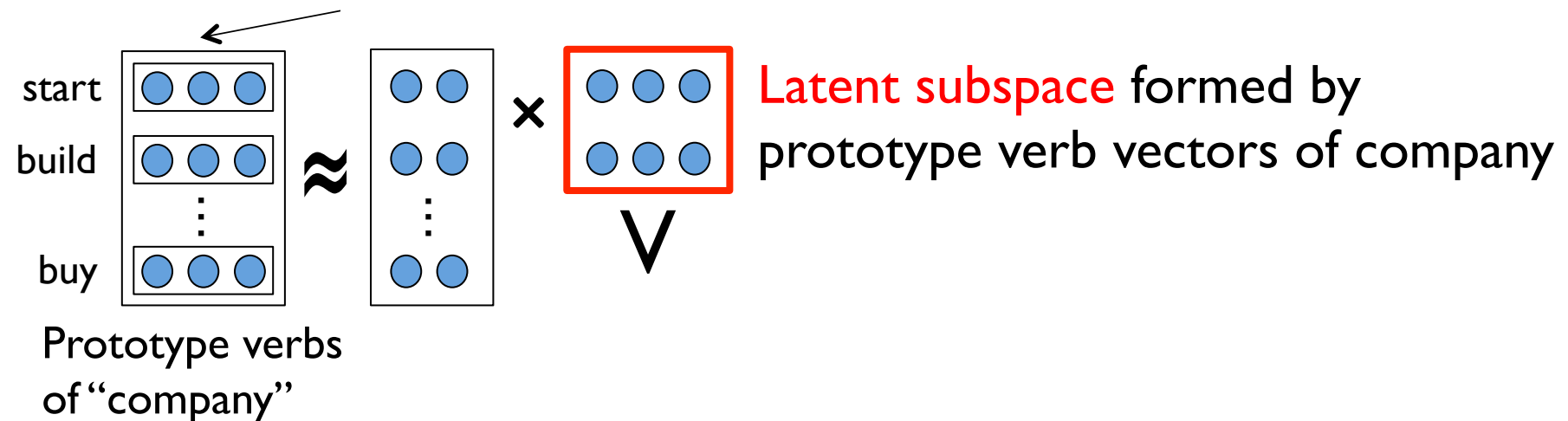
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Co-Compositionality with Prototype Projections

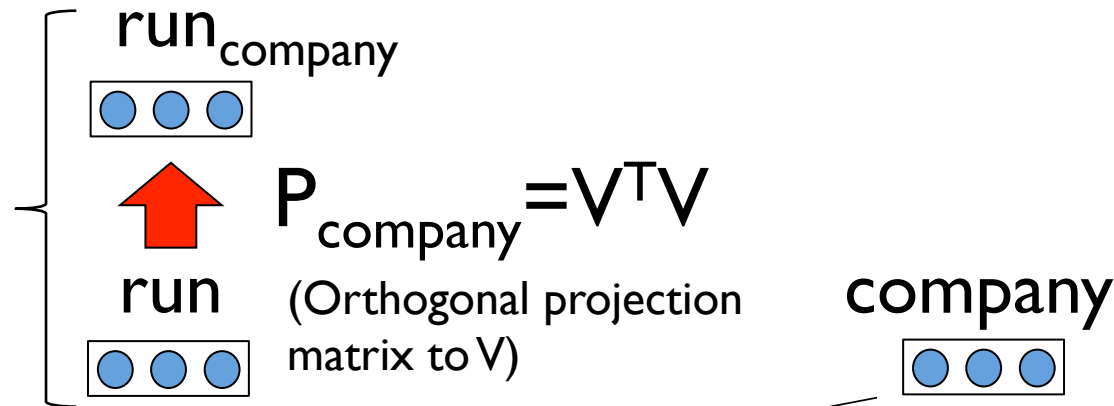


VerbOf

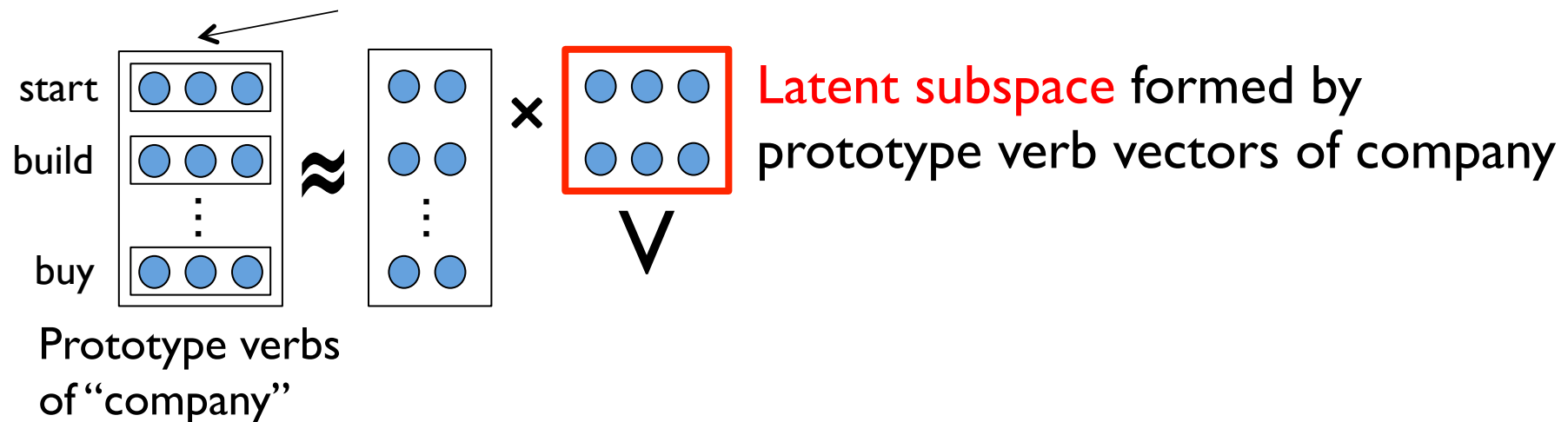


Co-Compositionality with Prototype Projections

Prototype Projection

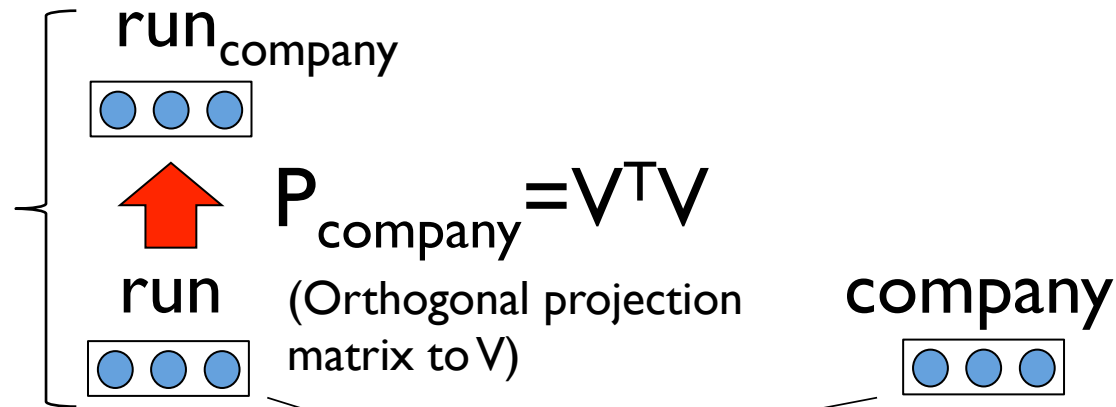


VerbOf



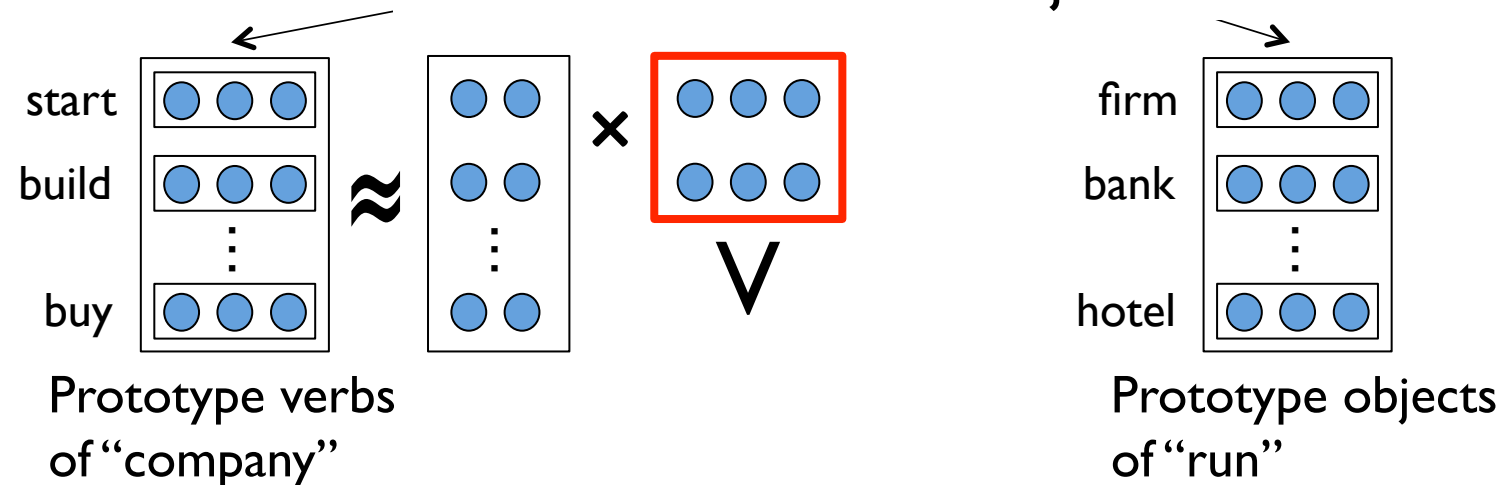
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Prototype Projection



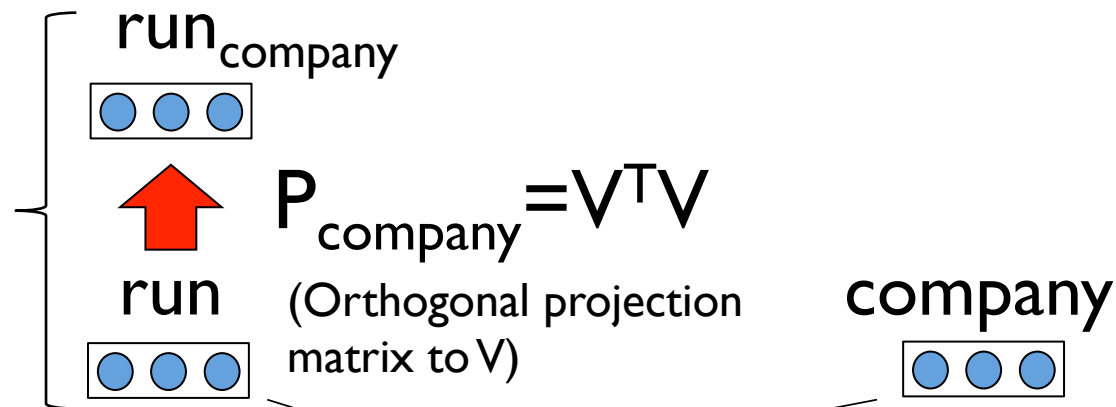
VerbOf

ObjectOf



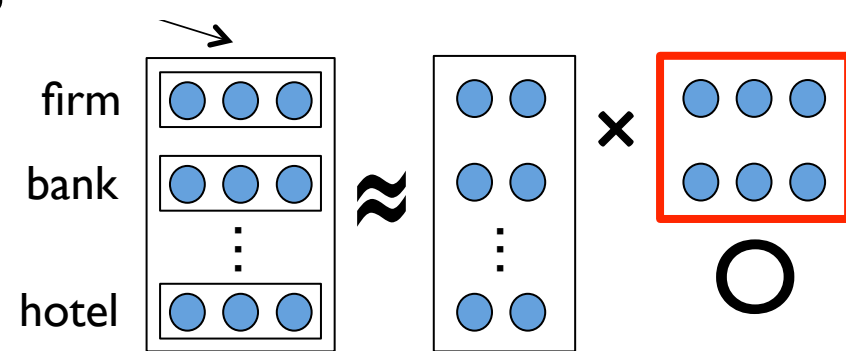
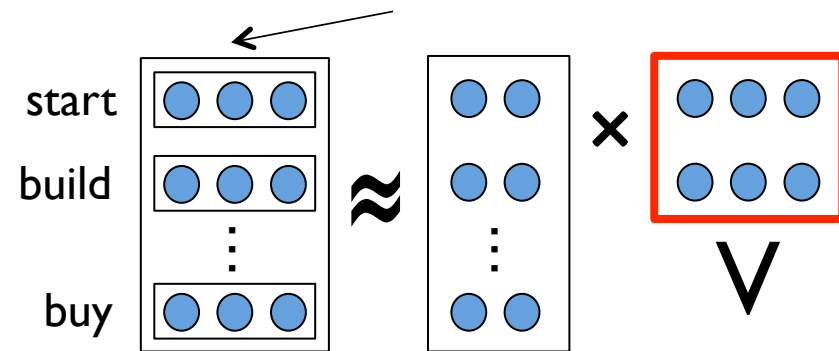
Co-Compositionality with Prototype Projections

Prototype Projection



VerbOf

ObjectOf

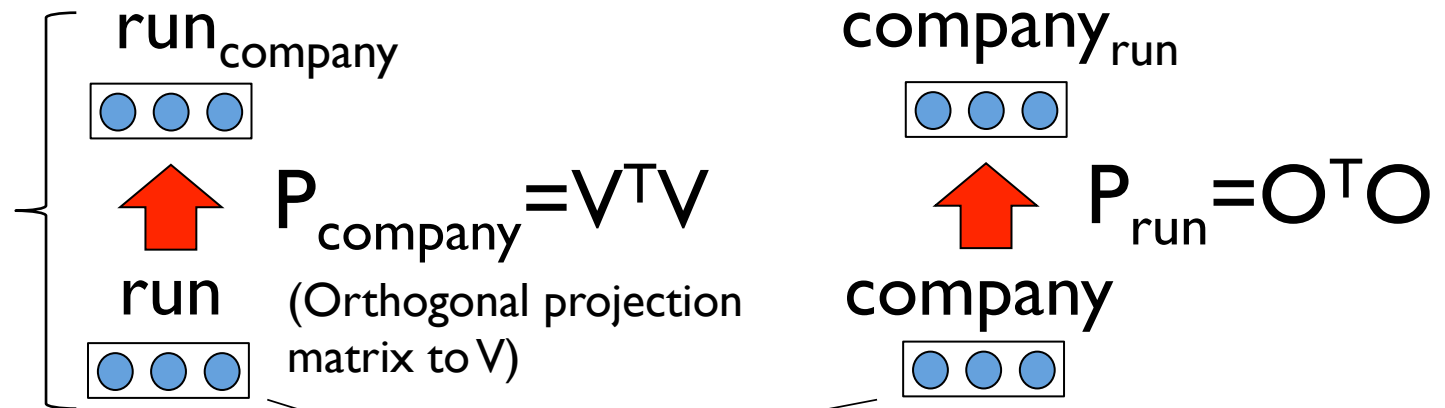


Prototype verbs
of "company"

Prototype objects
of "run"

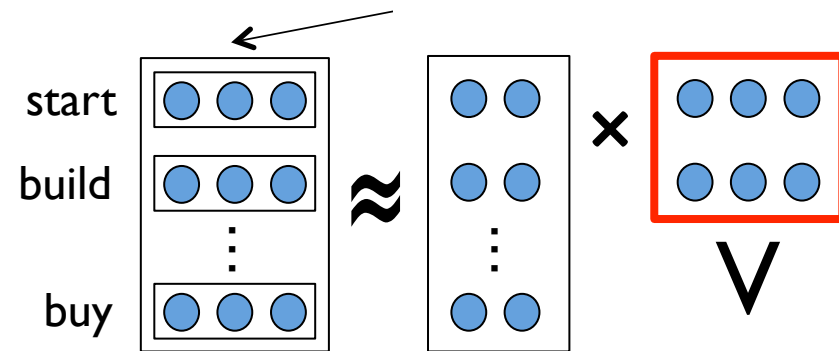
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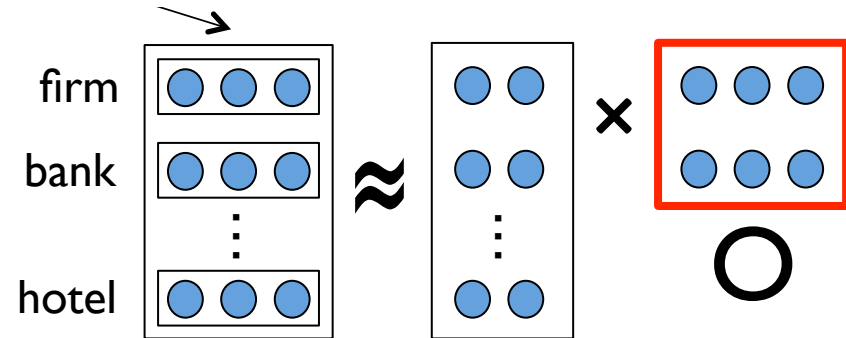


VerbOf

ObjectOf



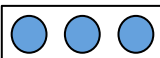
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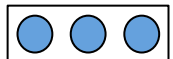
Co-Compositionality with Prototype Projections

Prototype Projection

operate = 

+

run_{company}





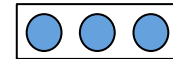
run



$$P_{\text{company}} = V^T V$$

(Orthogonal projection matrix to V)

company_{run}





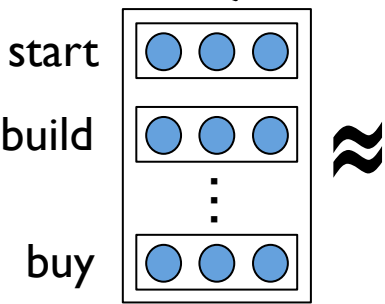
company



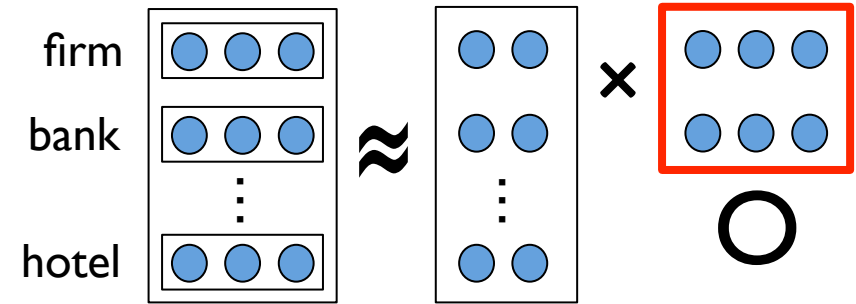
$$P_{\text{run}} = O^T O$$

VerbOf

ObjectOf

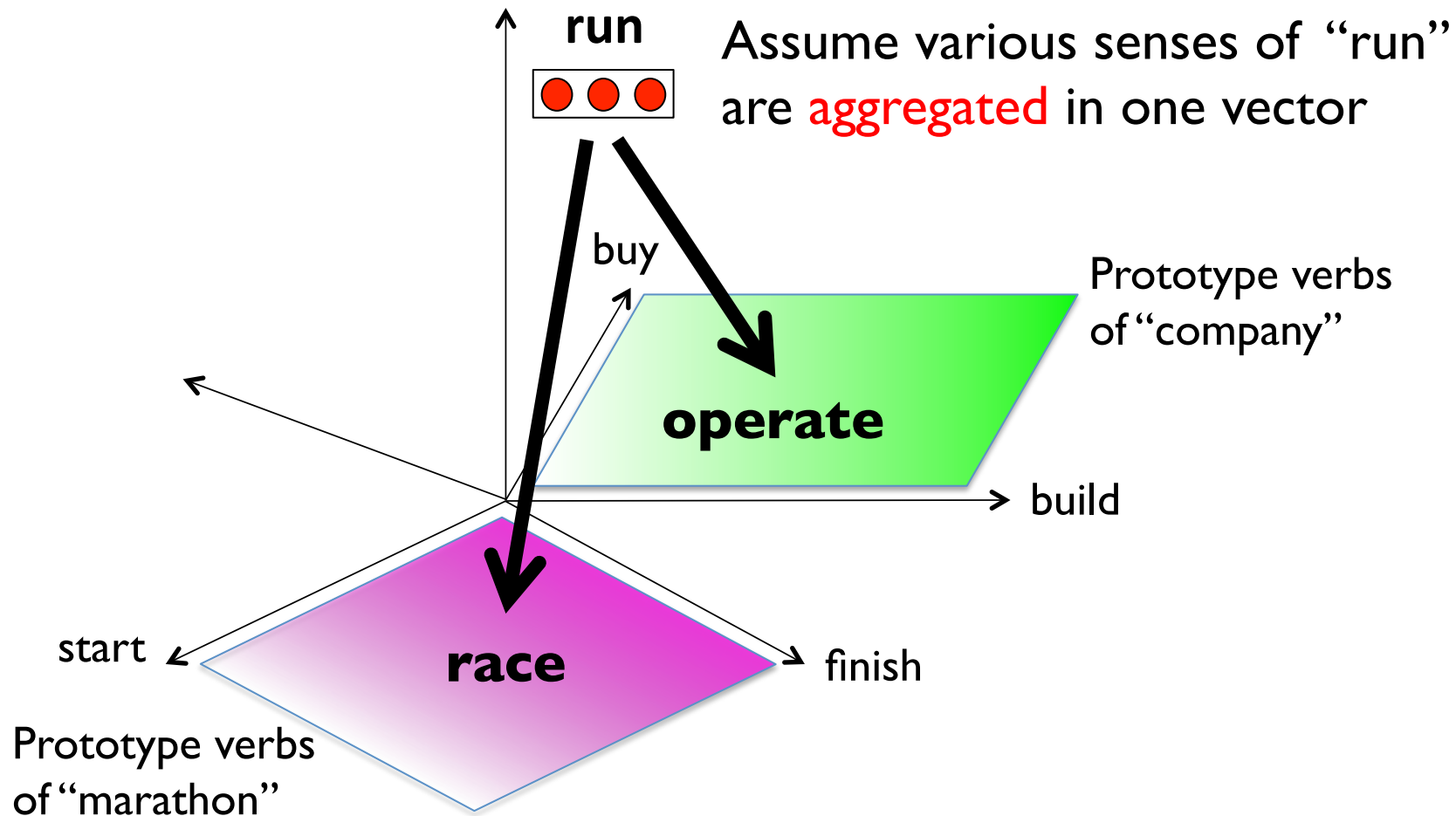


Prototype verbs of "company"



Prototype objects of "run"

Intuitive image of prototype projection



Tease out the proper semantics from aggregate representation **by projection to latent space**

Evaluation : Verb disambiguation in subject-verb-object triples

Evaluation dataset [Grefenstette and Sadrzadeh 11]

Subj-Verb-Obj	Landmark verb	Similarity of human judgment
People- run -company	operate	7
People- run -company	move	2

200 subject-verb-object triples judged by 25 participants

Evaluation : Verb disambiguation in subject-verb-object triples

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Final co-compositional vector for subject-verb-object

subj + cocompositioned(verb, obj)

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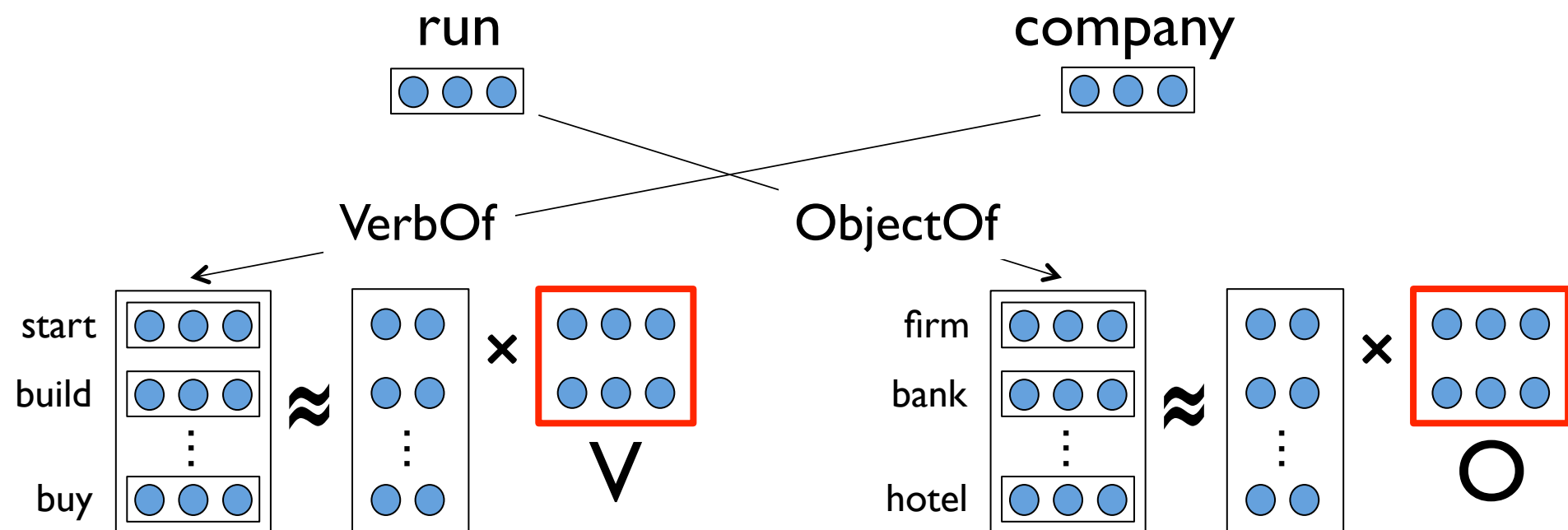
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 $subj + cocompositional(verb, obj)$

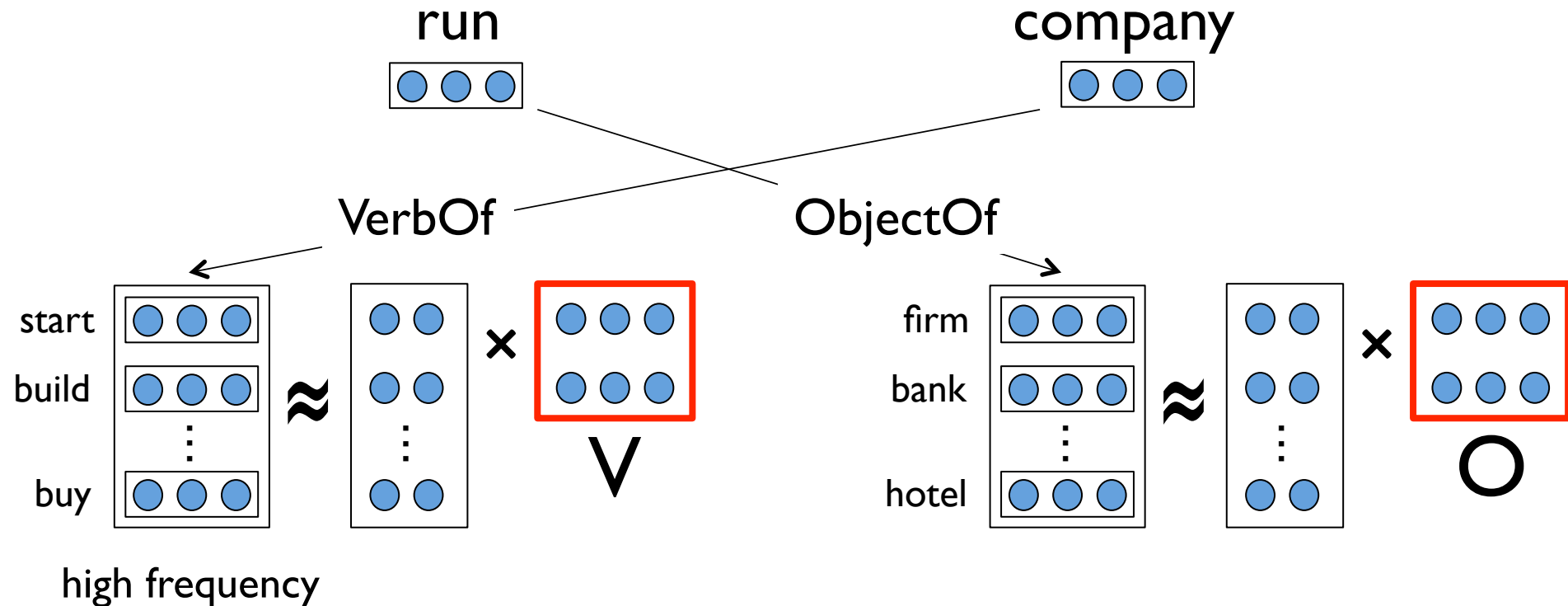
Models are evaluated by Spearman's rank correlation between vectors' computed similarity and human judgment

Implementation details



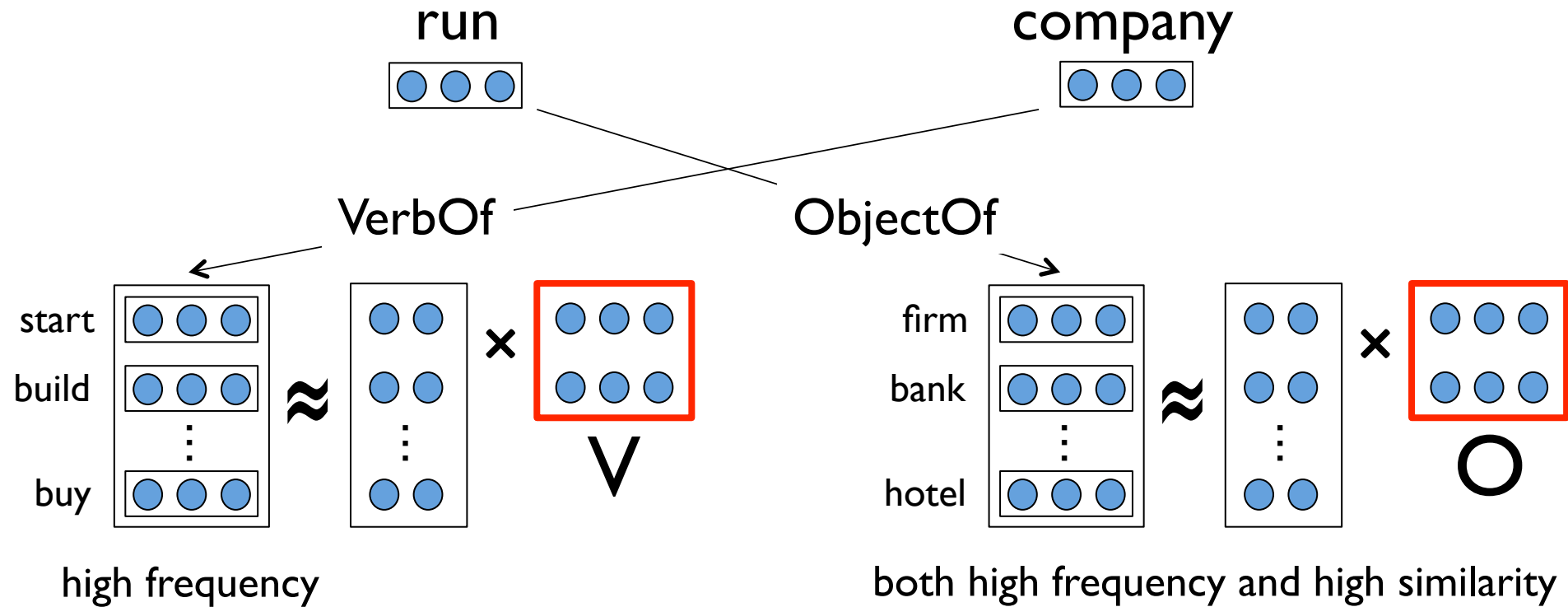
Extracted 20 prototype words from ukWaC corpus

Implementation details



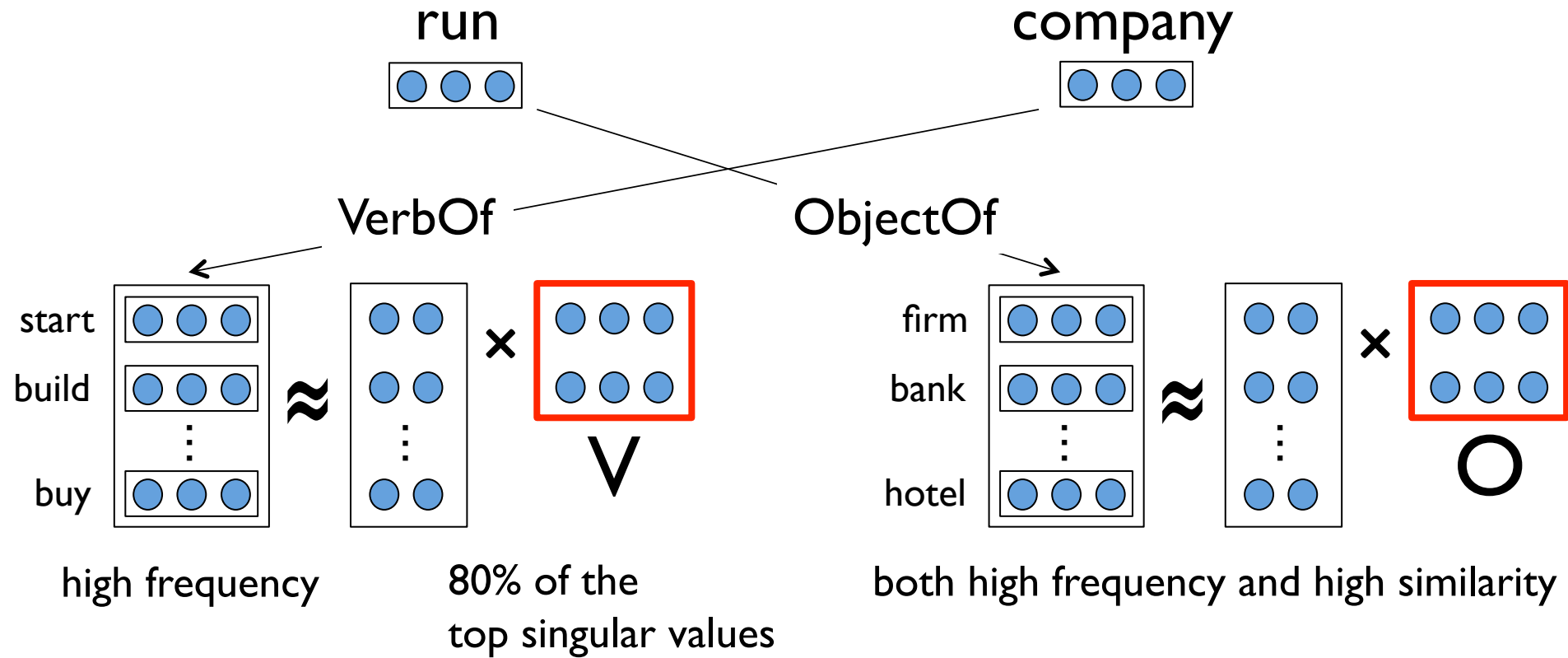
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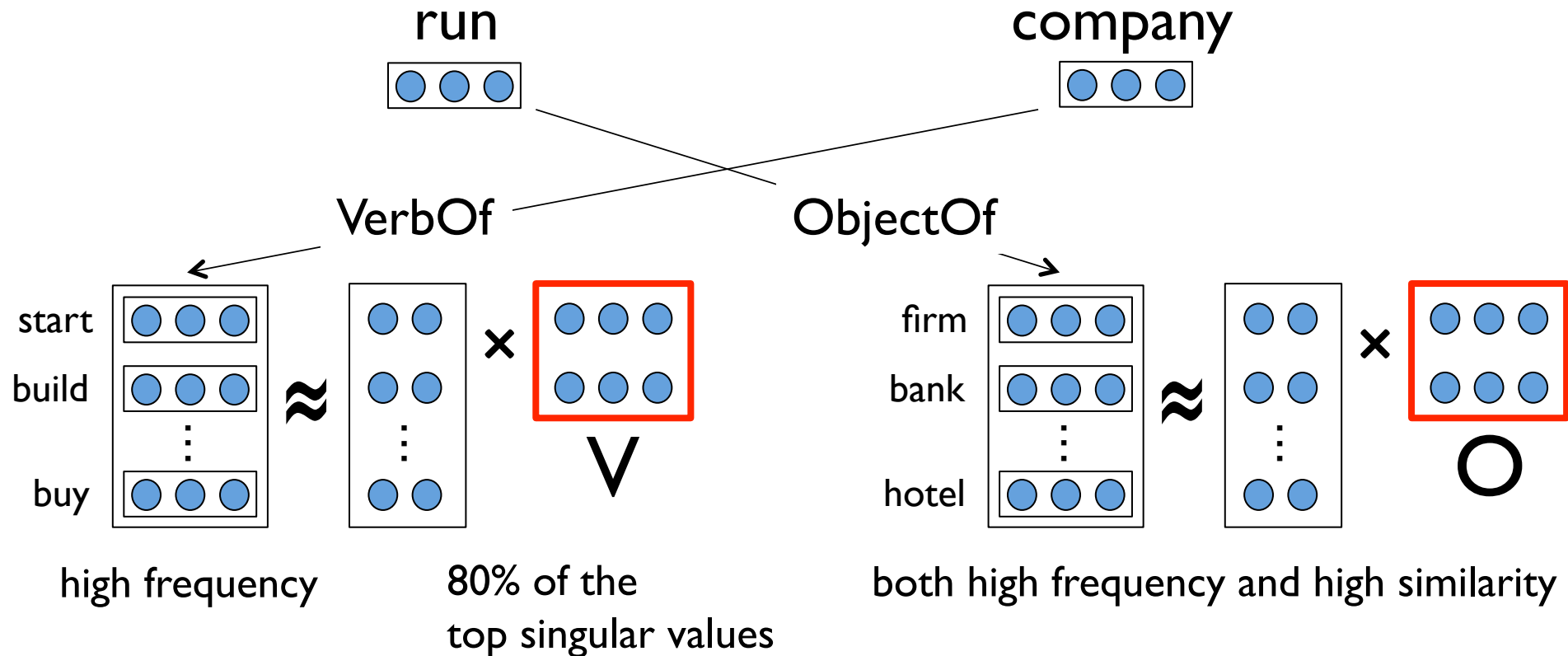
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Word representation [Blacoe and Lapata 12]

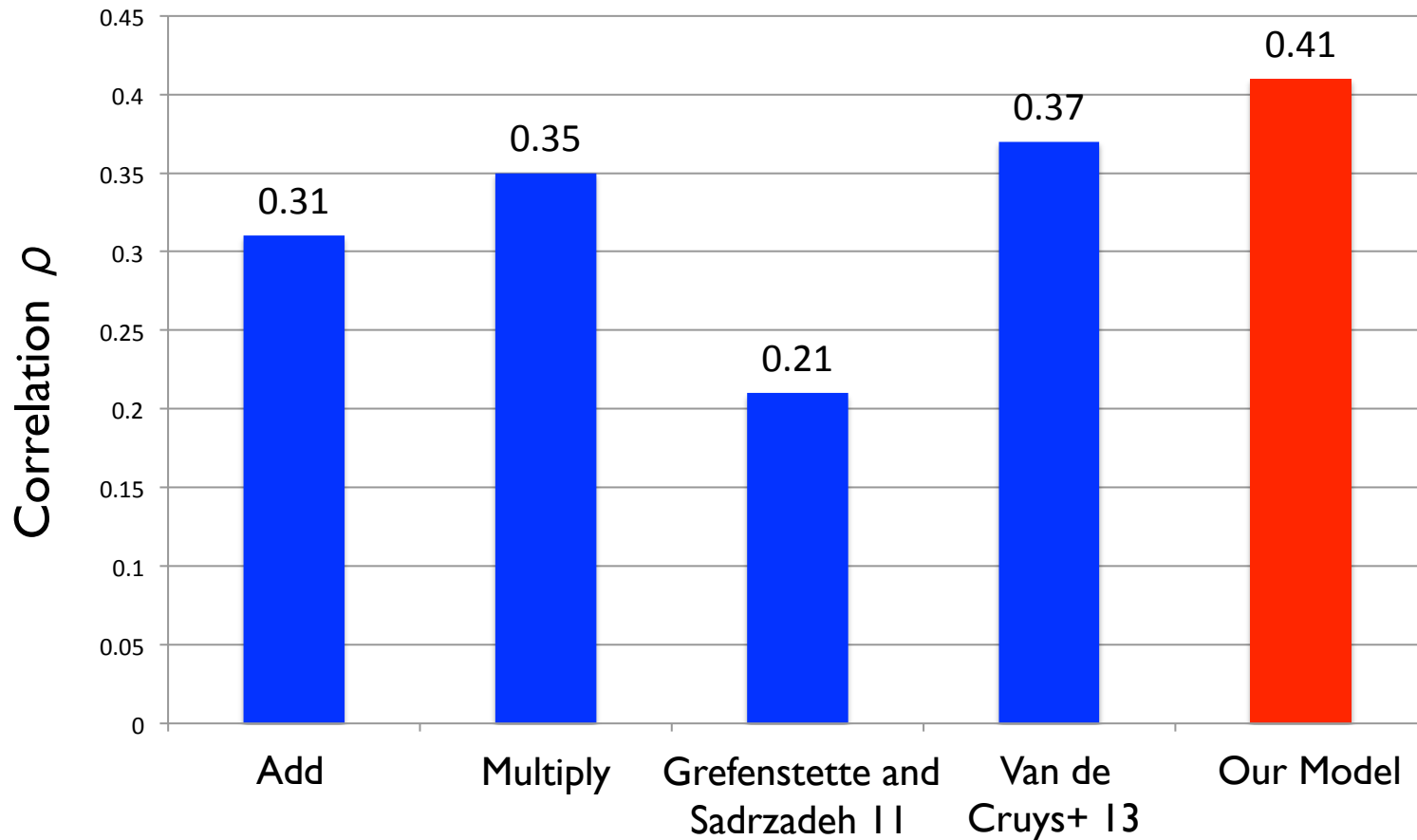
① Distributional vector (2000 dim) ② Neural vector (50 dim)

Baselines : Models compared to ours

Add [Mitchell and Lapata 08]	$sbj + verb + obj$
Multiply [Mitchell and Lapata 08]	$sbj \times verb \times obj$
Grefenstette and Sadrzadeh 11	Mathematical model based on abstract categorical framework
Van de Cruys+13	Multi-way interaction model based on non-negative matrix factorization

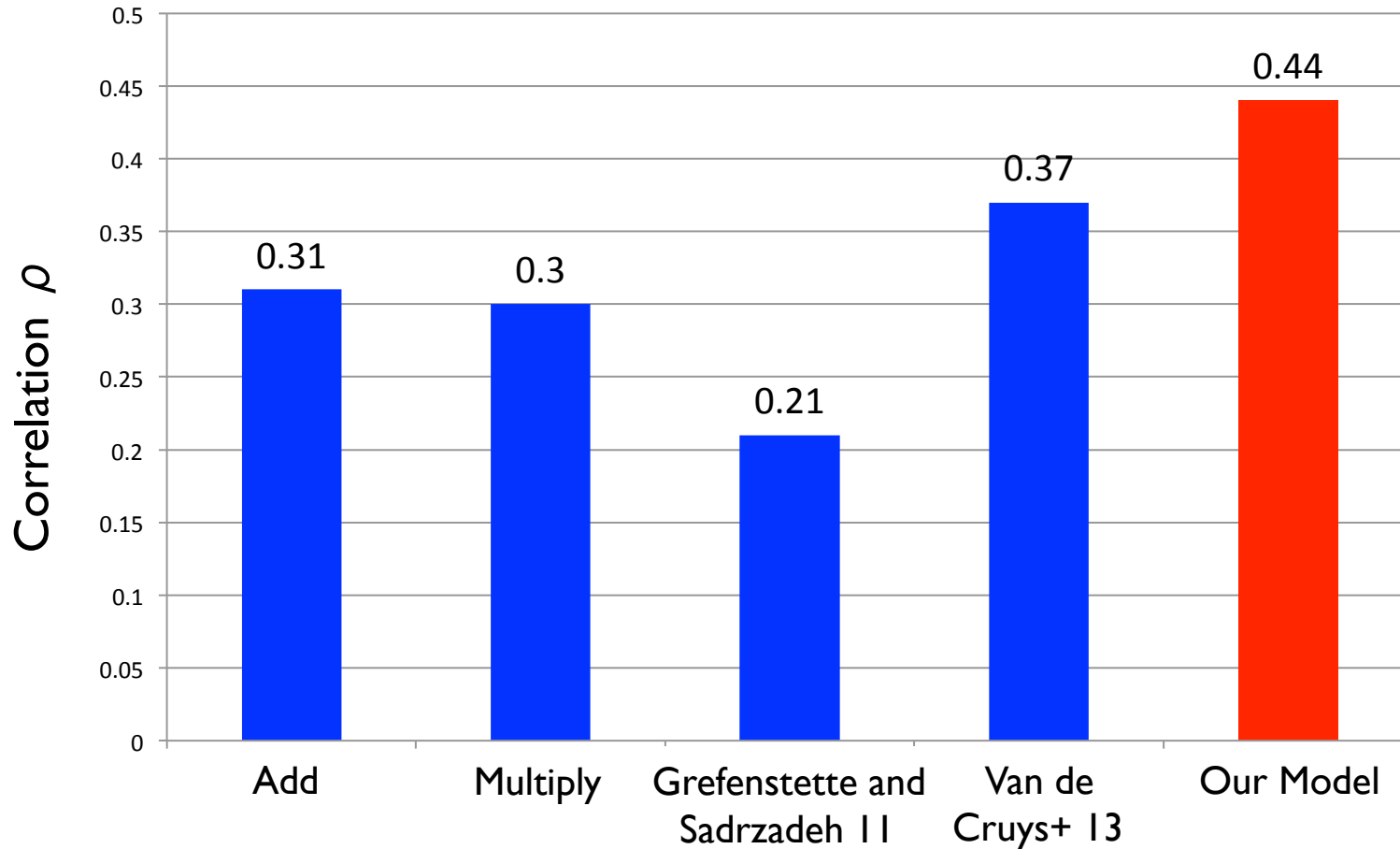
Correlation with human judgment (Distributional vector)

Achieves high performance ($\rho = 0.41$)



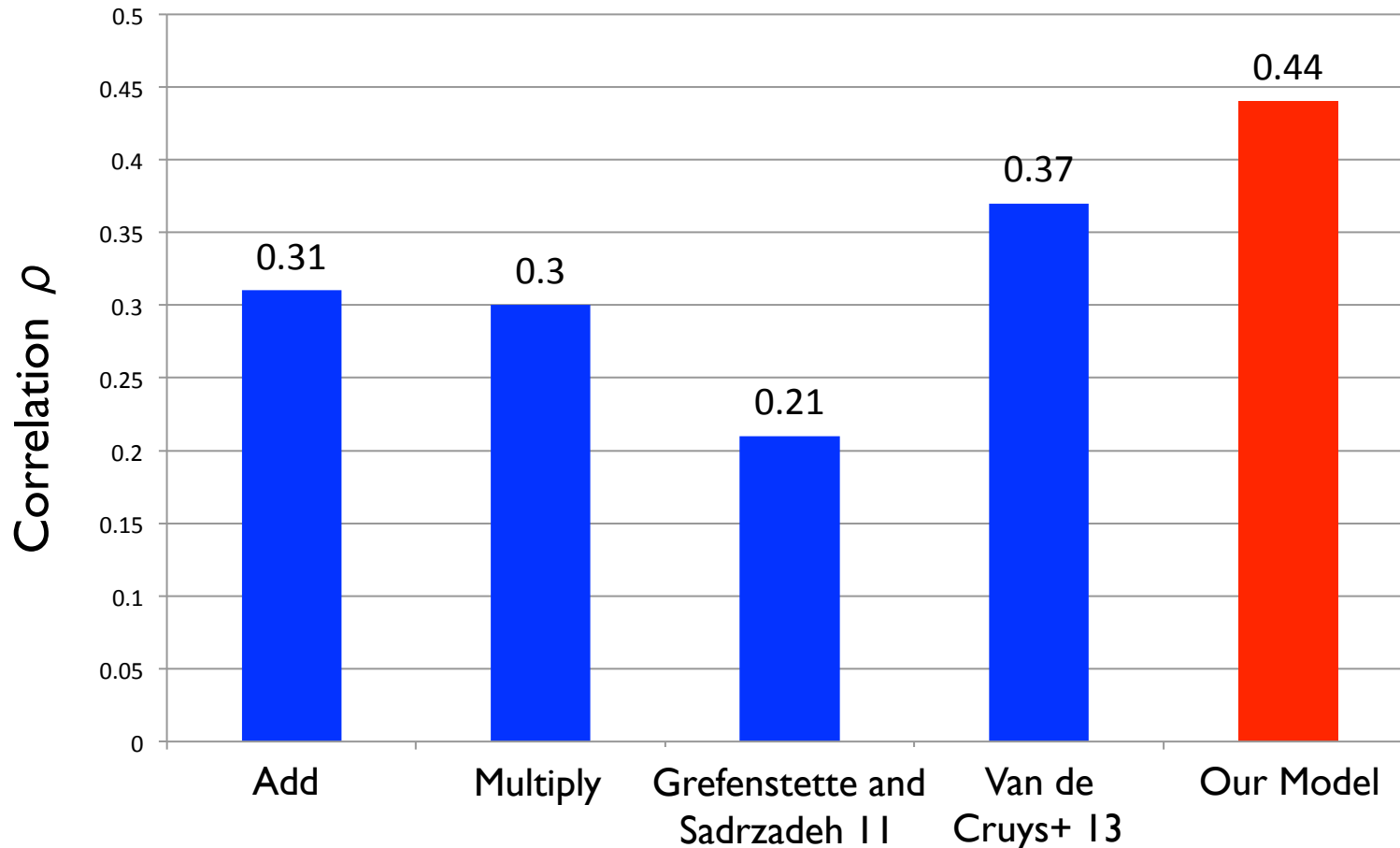
Correlation with human judgment (Neural vector)

State of the art performance ($\rho = 0.44$)



Correlation with human judgment (Neural vector)

State of the art performance ($\rho = 0.44$)



Co-Compositionality is useful for word sense disambiguation

Prototype projection is **effective implementation** for Co-Compositionality

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Unsupervised word vector
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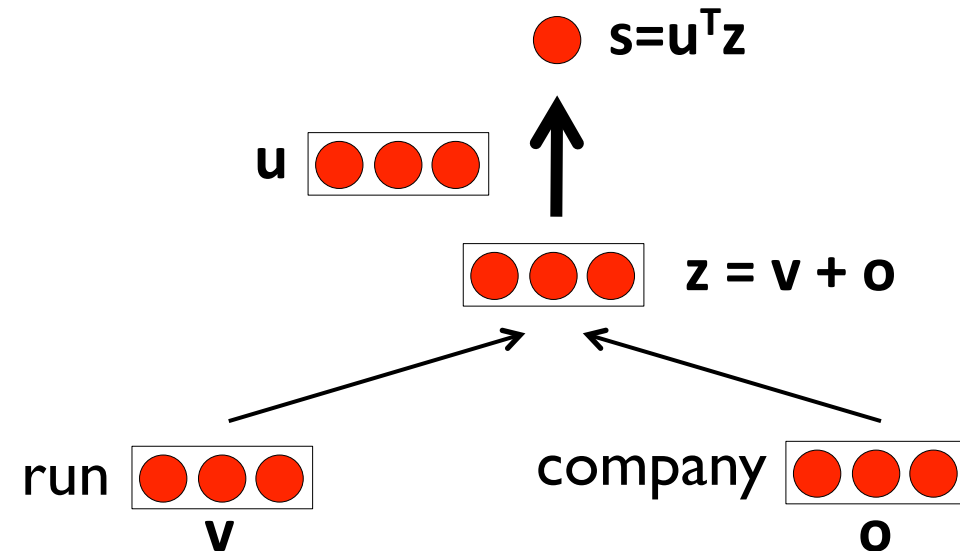
Unsupervised word vector
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Compositional Neural Language Model

Re-training word representation with **decomposition of phrase vector**

Compositional Neural Language Model

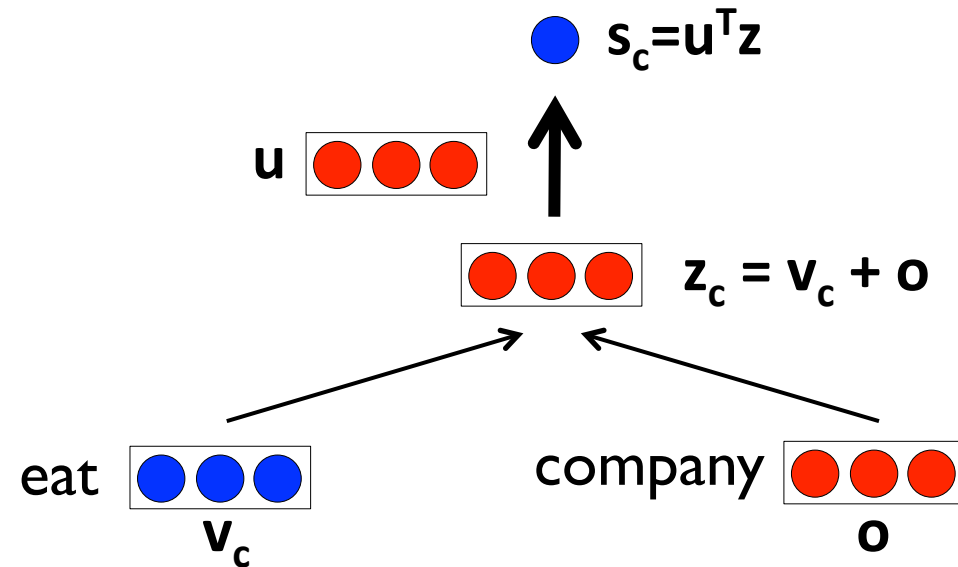
Re-training word representation with **decomposition of phrase vector**



① Compute the score s of correct phrase

Compositional Neural Language Model

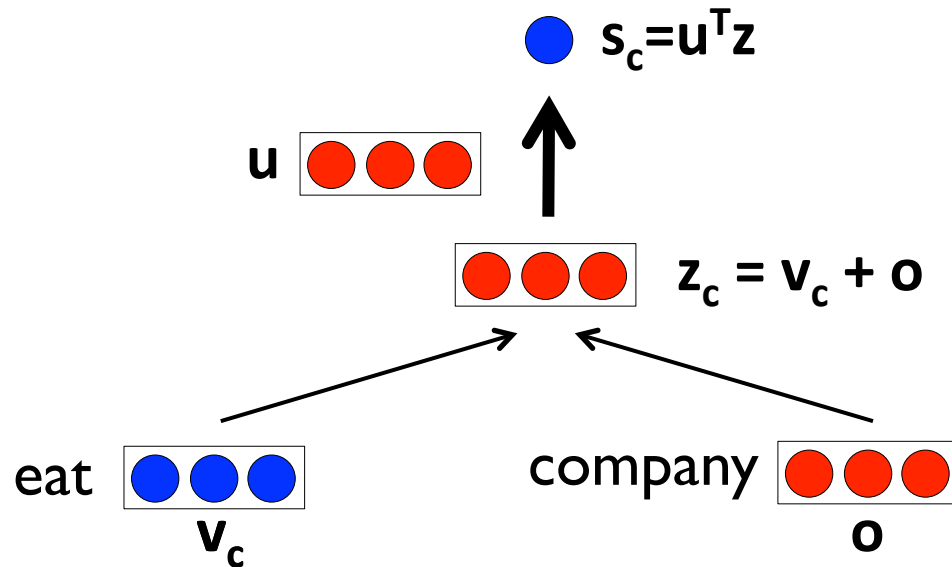
Re-training word representation with **decomposition of phrase vector**



- ① Compute the score s of correct phrase
- ② Compute the score s_c of corrupted incorrect phrase

Compositional Neural Language Model

Re-training word representation with **decomposition of phrase vector**



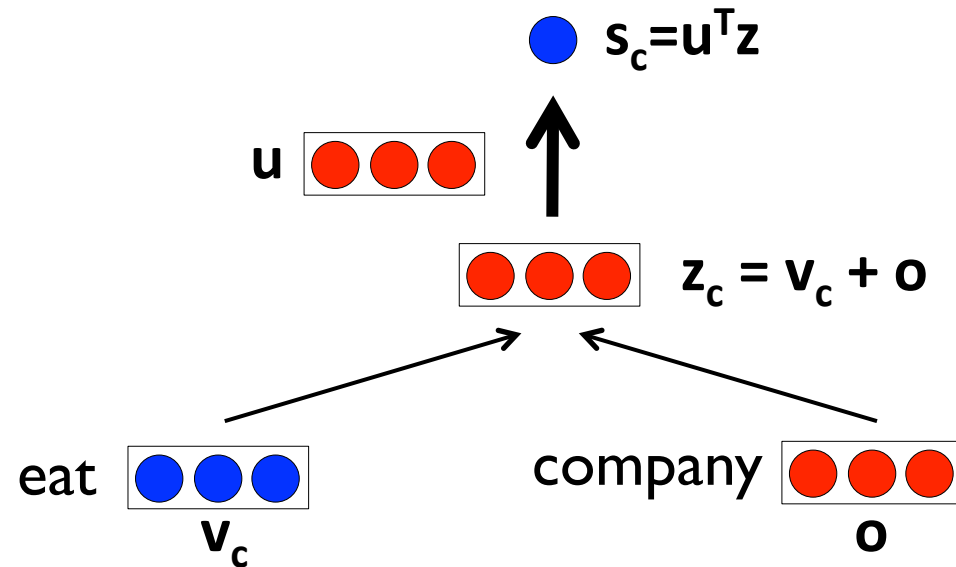
- ① Compute the score s of correct phrase
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$$J = \max(0, 1 - s + s_c)$$

Correct score $>$ Incorrect score

Compositional Neural Language Model

Re-training word representation with **decomposition of phrase vector**



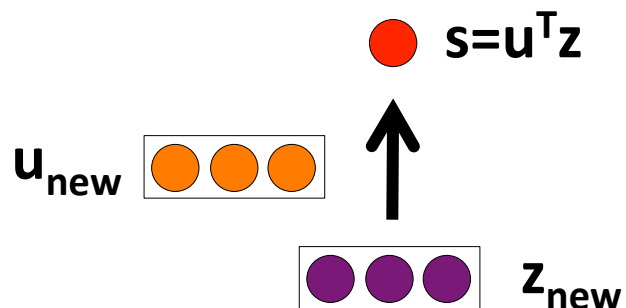
$$J = \max(0, 1 - s + s_c)$$

Correct score $>$ Incorrect score

- ① Compute the score s of correct phrase
- ② Compute the score s_c of corrupted incorrect phrase
- ③ Minimize cost function by SGD, $u \rightarrow u_{\text{new}}$, $z \rightarrow z_{\text{new}}$

Compositional Neural Language Model

Re-training word representation with **decomposition of phrase vector**



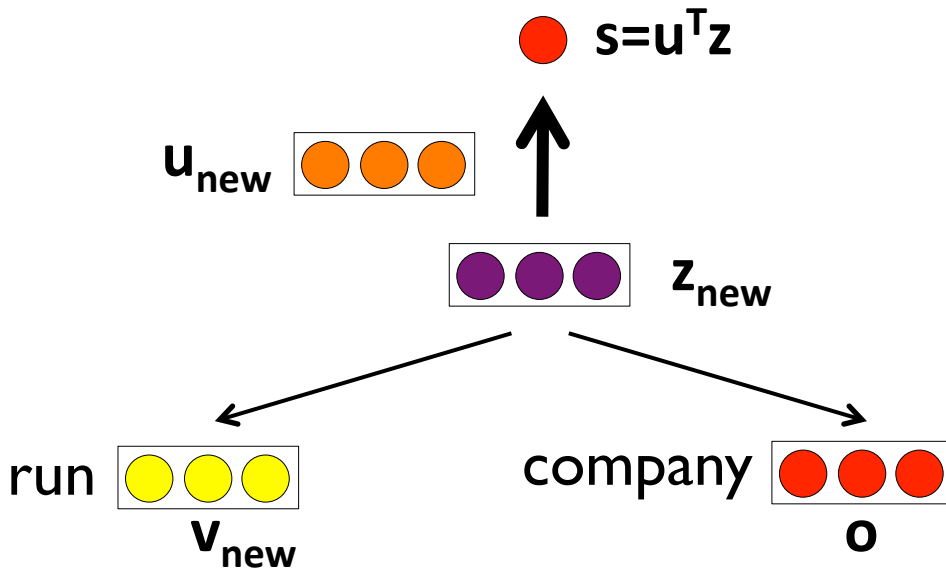
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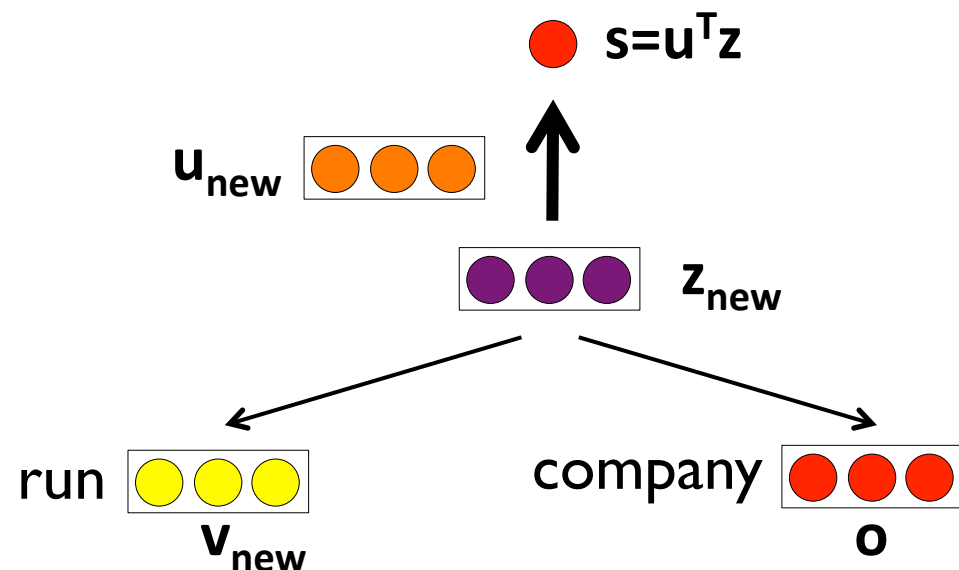
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Correct score > **Incorrect score**

- ① Compute the score s of correct phrase
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- ③ Minimize cost function by SGD, $u \rightarrow u_{new}$, $z \rightarrow z_{new}$
- ④ New verb vector is $v_{new} = z_{new} - o$

Compositional Neural Language Model

Re-training word representation with **decomposition of phrase vector**



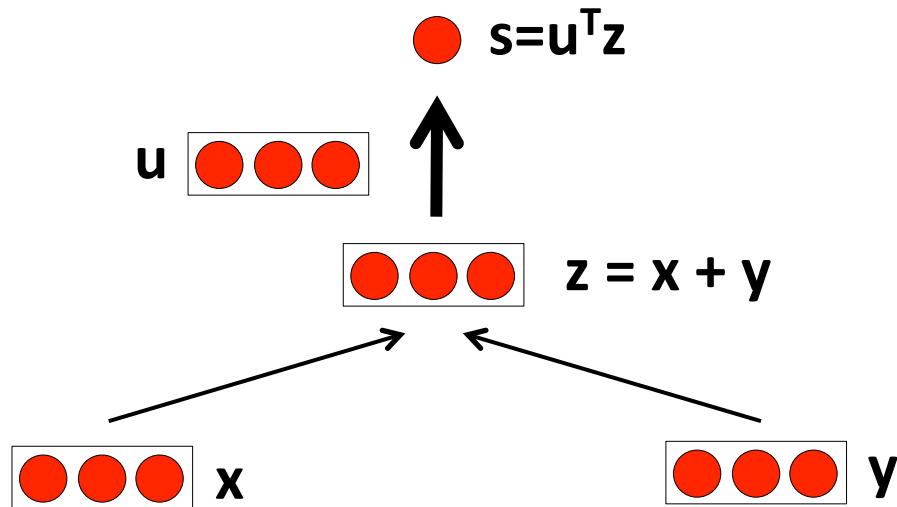
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Correct score > **Incorrect score**

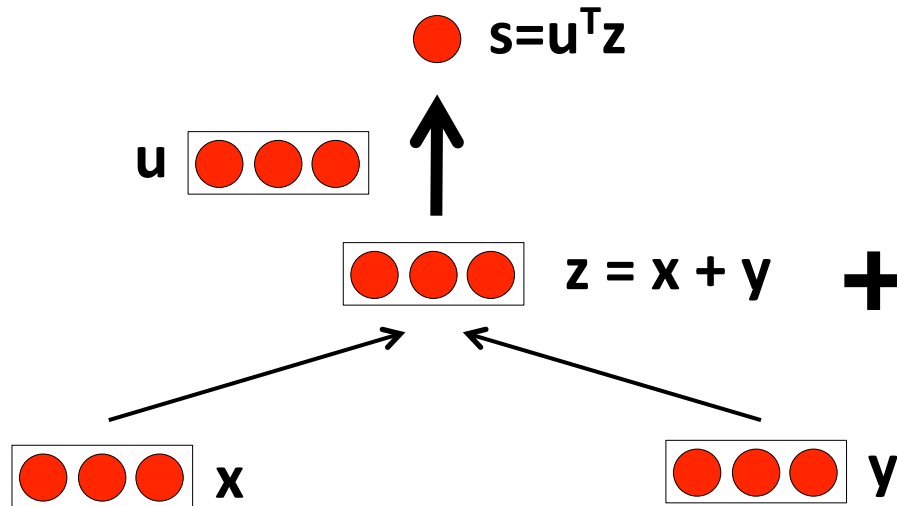
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- ④ New verb vector is $\mathbf{v}_{\text{new}} = \mathbf{z}_{\text{new}} - \mathbf{o}$

New word representations **considering compositionality**

Compositional Neural Language Model

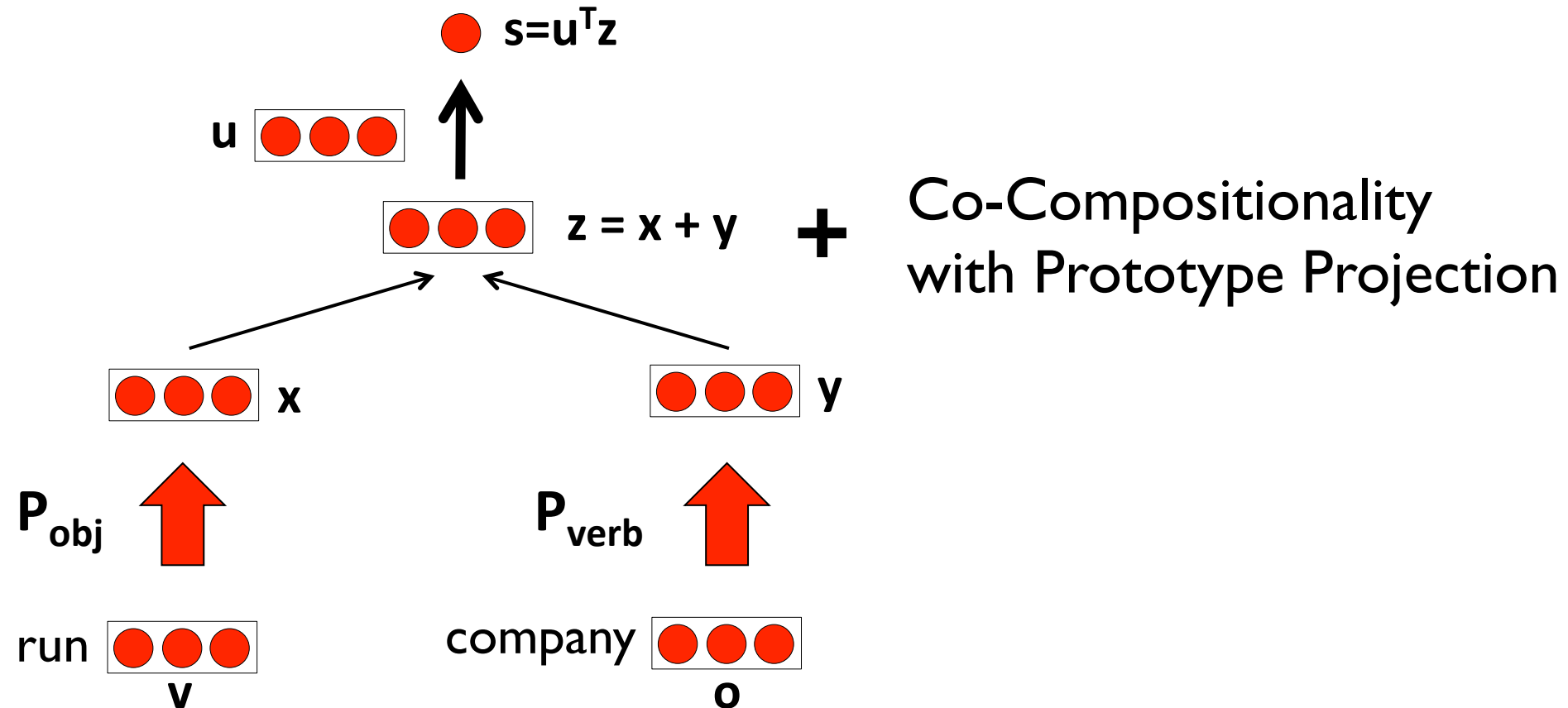


Compositional Neural Language Model



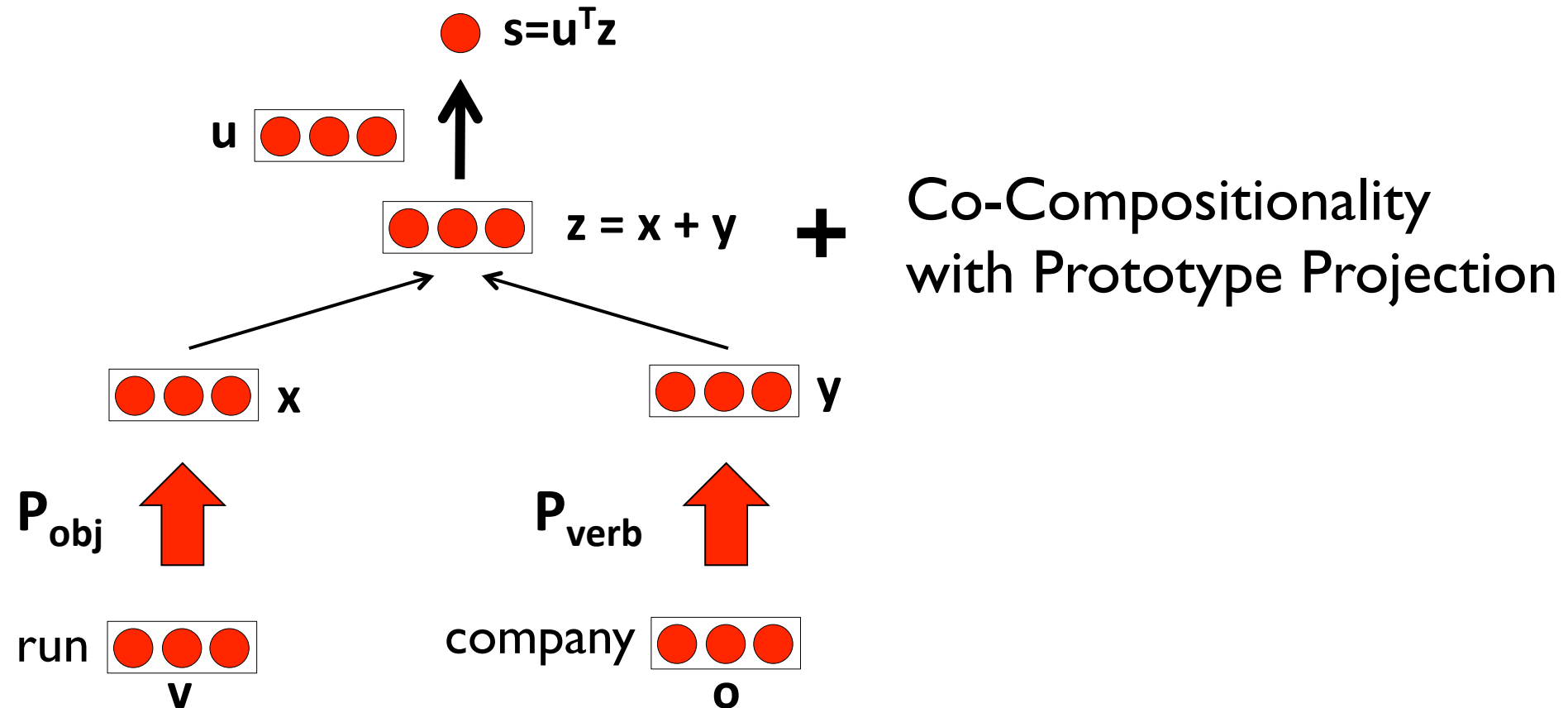
Co-Compositionality
with Prototype Projection

Compositional Neural Language Model



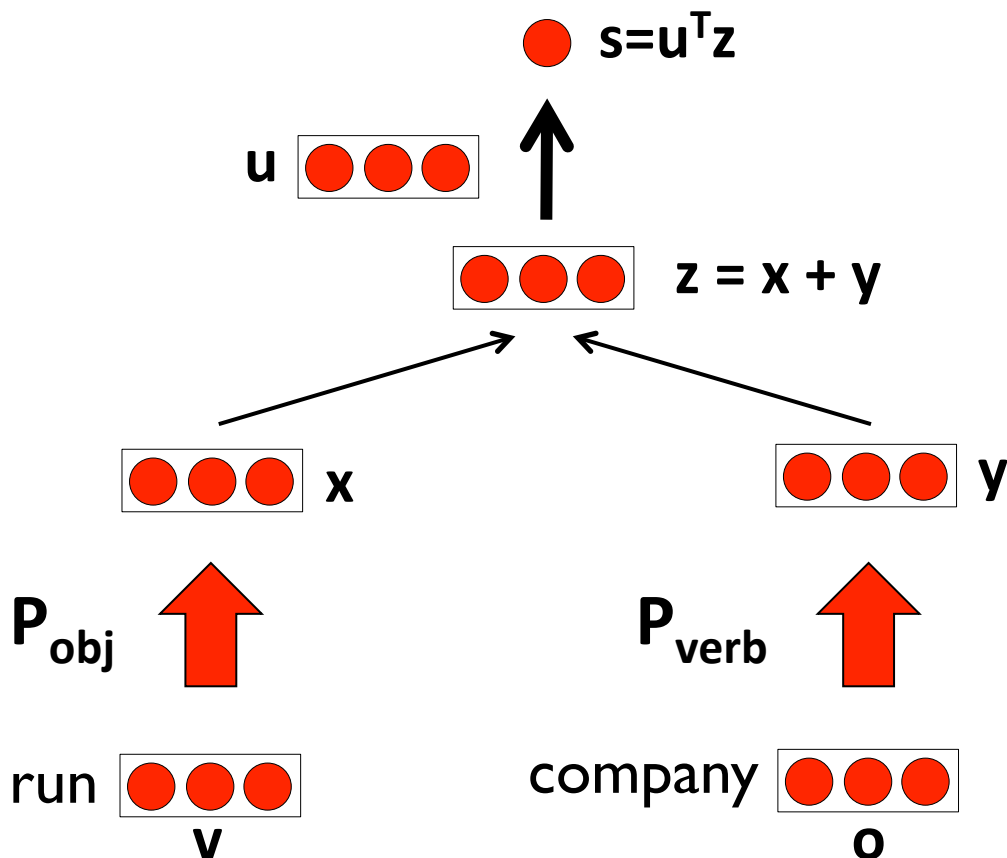
Co-Compositional Neural Language Model

Compositional Neural Language Model **with Prototype Projection**



Co-Compositional Neural Language Model

Compositional Neural Language Model **with Prototype Projection**



① Prototype projection for both verb and object

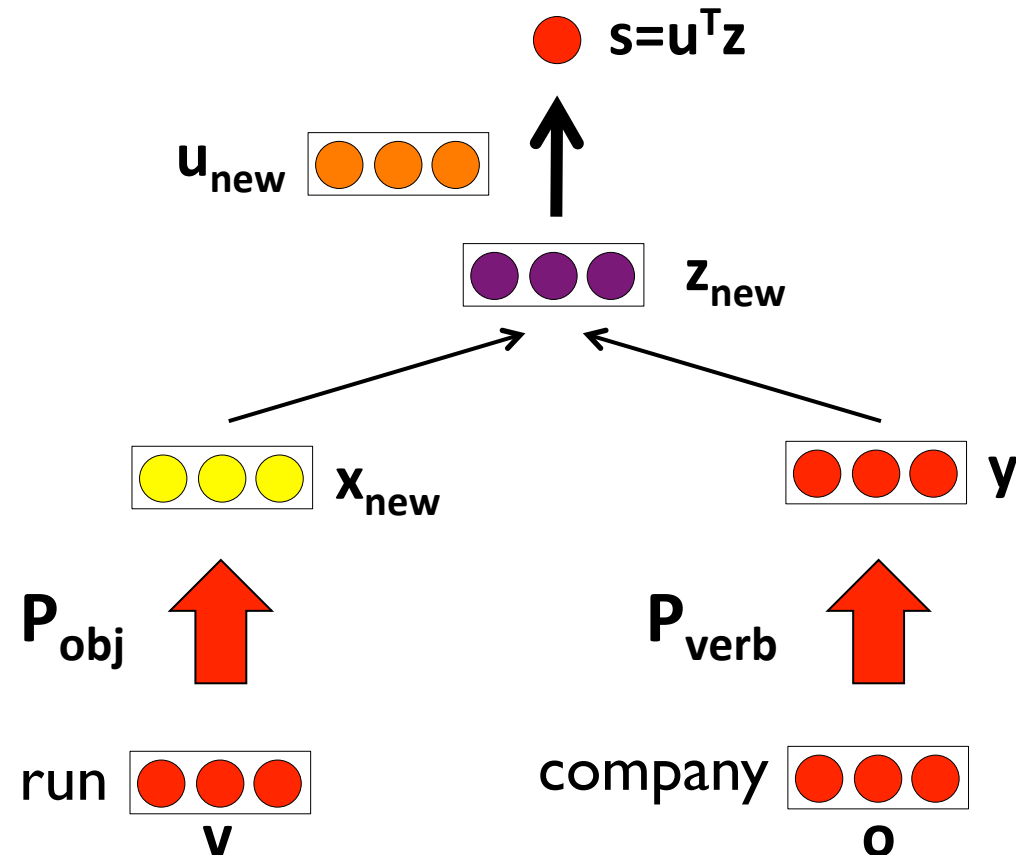
② Optimize parameters with same method as Compositional NLM

③ Minimize

$$\min_v \left(\|x_{new} - P_{obj} v\|^2 + \lambda \|v\|^2 \right)$$

Co-Compositional Neural Language Model

Compositional Neural Language Model **with Prototype Projection**



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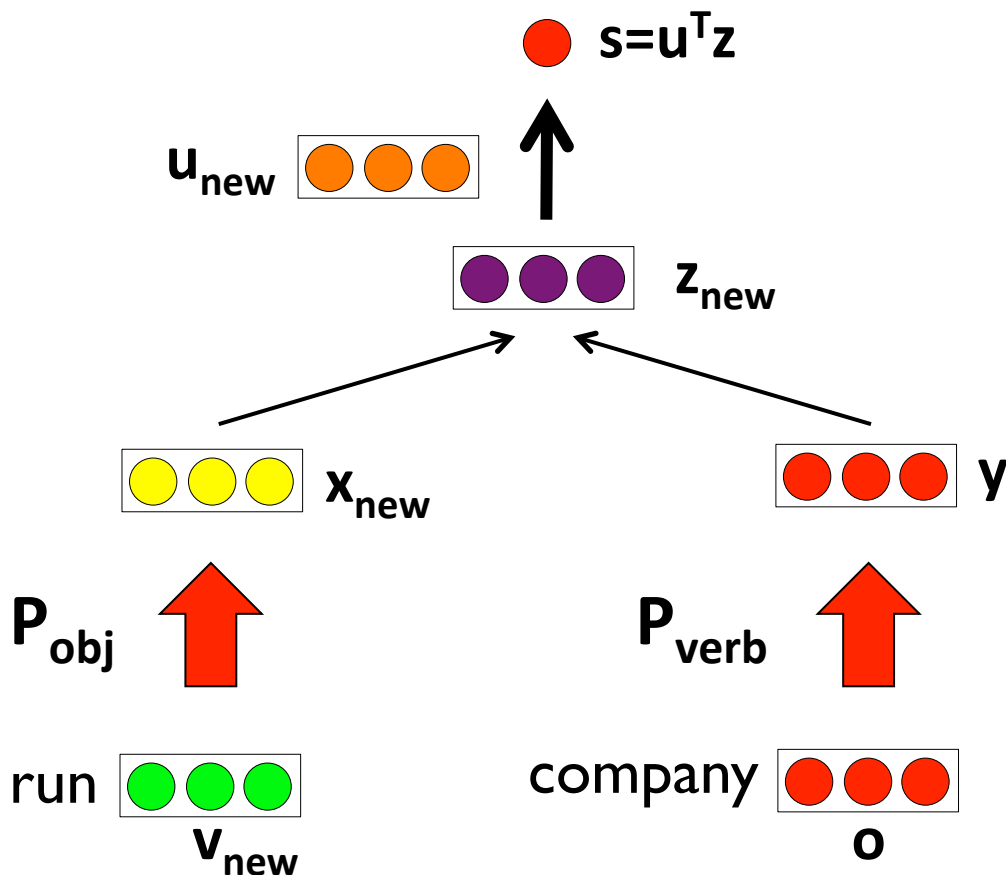
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Co-Compositional Neural Language Model

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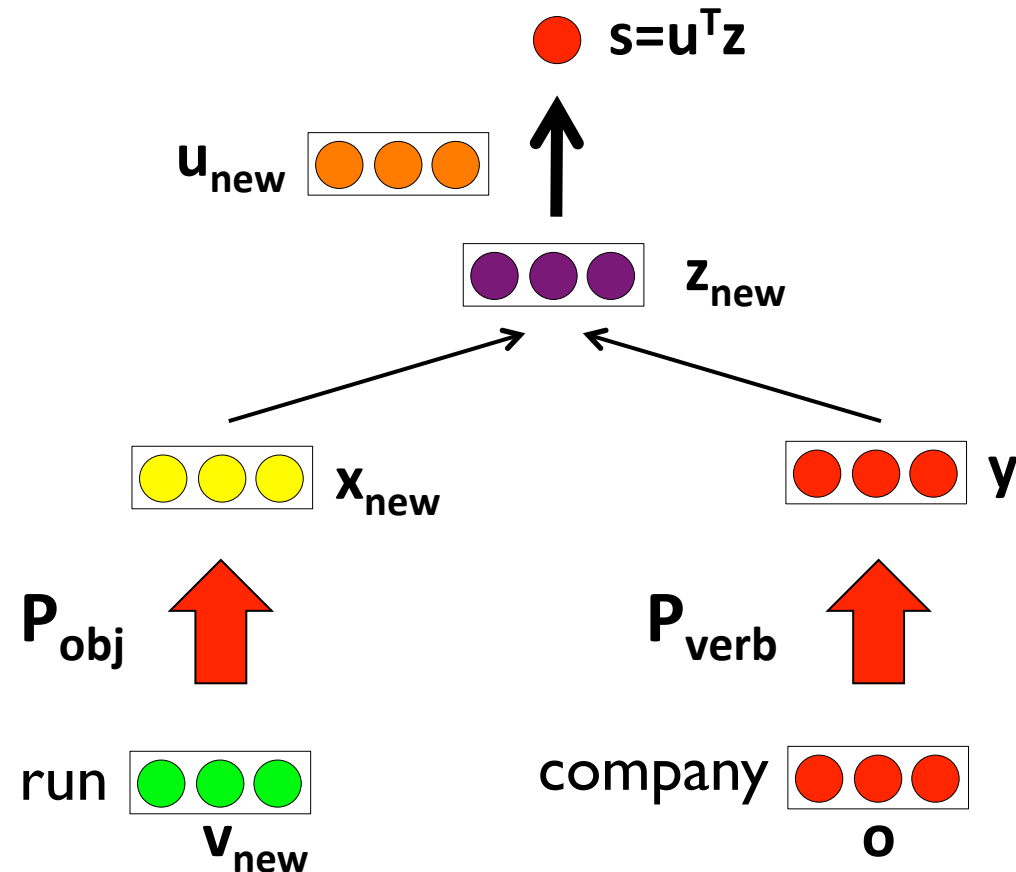
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Co-Compositional Neural Language Model

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New word representations **considering co-compositionality**

Evaluation : Verb disambiguation [Grefenstette and Sadrzadeh 11]

Original neural vector [Blacoe and Lapata 12]

VS.

Re-trained neural vector with our learning models

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Training data

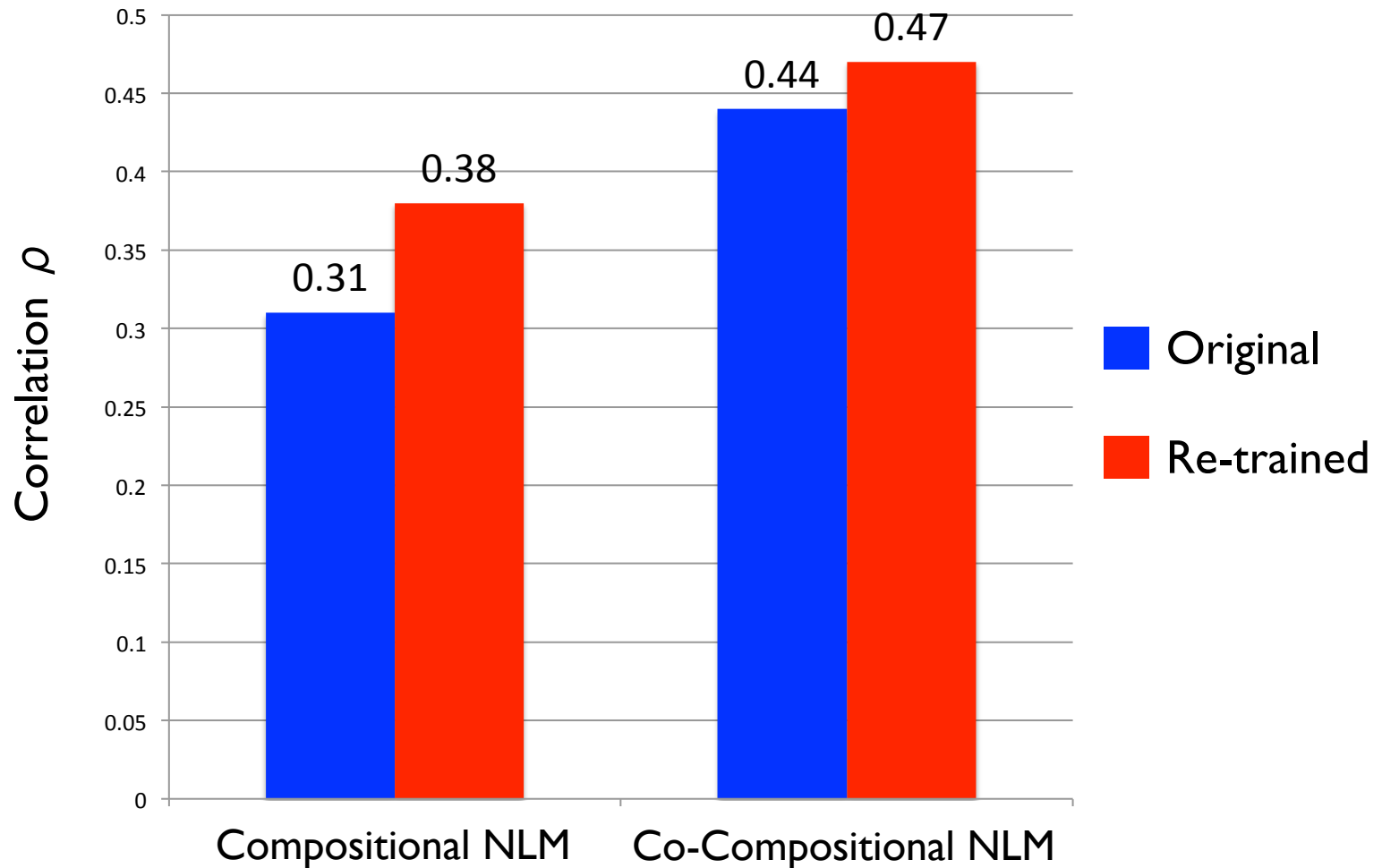
Extracted **5000 Verb-Obj pairs** from ukWaC corpus

Hyper-parameters

Learning rate: 0.01, Regularization: 10^4

20 iterations (One iteration is one run through the training data)

Correlation with human judgment (Re-trained neural vector)

New state of the art performance ($\rho = 0.47$)**Higher performance** with re-trained word representation

Conclusion

New model of
compositionality
in word vector space

Co-Compositionality with Prototype Projection

Unsupervised word vector
re-training algorithm
considering compositionality

Compositional & Co-Compositional Neural Language Models
Achieve state of the art on verb disambiguation task

Examples

verb	object	landmark	similarity(verb, landmark)	similarity(projected verb, landmark)
run	company	operate	0.40	0.70
meet	criterion	satisfy	0.49	0.71
spell	name	write	0.04	0.50

Table 1: Examples of verb-object pairs. Original verb and landmark verb similarity, prototype projected verb and landmark verb similarity, as measure by cosine using Collobert and Weston’s word embeddings. *Meet* has a abstract meaning itself, but after prototype projection with matrix constructed by word vectors of $W(VerbOf, criterion)$, *meet* is more close to meaning of *satisfy*.

Results of the different compositionality models

Model	ρ
Grefenstette and Sadrzadeh (2011)	0.21
Add (SDS)	0.31
Add (NLM)	0.31
Multiply (SDS)	0.35
Multiply (NLM)	0.30
Van de Cruys et al. (2013)	0.37
Erk and Padó (SDS)	0.39
Erk and Padó (NLM)	0.03
Co-Comp with f =Add (SDS)	0.41
Co-Comp with f =Add (NLM)	0.44
Co-Comp with f =Multiply (SDS)	0.37
Co-Comp with f =Multiply (NLM)	0.35
Upper bound	0.62

Table 3: Results of the different compositionality models on the similarity task. The number of prototype words $m = 20$ in all our models. Our model (f =Addition and NLM) achieves the new state-of-the-art performance for this task ($\rho = 0.44$).

The number of prototype words

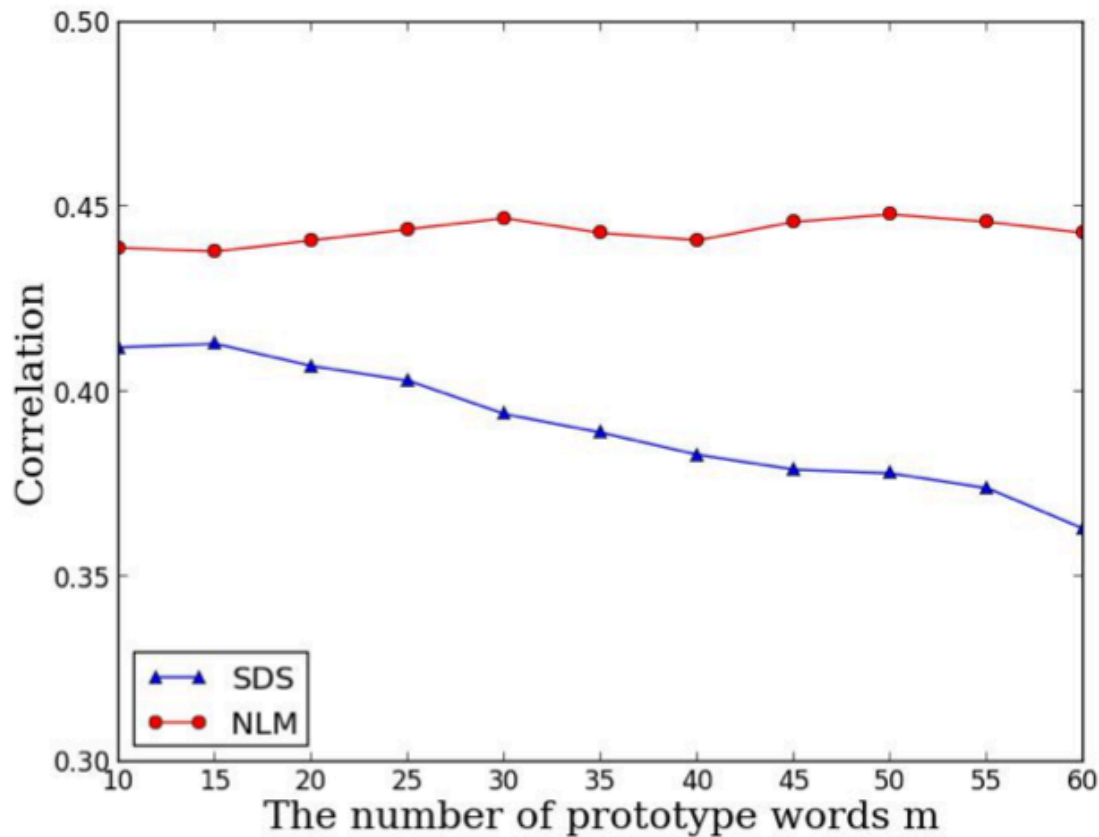


Figure 5: The relation between the number of prototype words and correlation of SDS or NLM. In general, NLM has higher correlation than SDS and is more robust across the m .

Variations in model configuration

Subj	Verb	Obj	NLM ρ	SDS ρ
prpj	prpj	prpj	0.39	0.37
+	prpj	prpj	0.44	0.41
	prpj	prpj	0.45	0.41
+	prpj	+	0.43	0.38
	prpj	+	0.43	0.38
+	+	+	0.31	0.31

Table 5: Variants of the full co-compositional model, based on how subject, verb, and object vector representations are included. prpj indicates that prototype projection is used. + indicates that the vector is added without projection first. Blank indicates that the vector is not used in the final compositional score.

Composition operator and parameter

Composition Operator	Parameter
Add: $w_1u + w_2v$	$w_1, w_2 \in \mathbb{R}$
Multiply: $u^{w_1} \odot v^{w_2}$	$w_1, w_2 \in \mathbb{R}$
FullAdd: $W_1u + W_2v$	$W_1, W_2 \in \mathbb{R}^{n \times n}$
LexFunc: A_uv	$A_u \in \mathbb{R}^{n \times n}$
FullLex: $\sigma([W_1A_uv, W_2A_vu])$	$A_u, A_v \in \mathbb{R}^{n \times n}$
	$W_1, W_2 \in \mathbb{R}^{n \times n}$
Ours (Add): $P_{(R,v)}u + P_{(R,u)}v$	SVD's (m, k)
Ours (Mult): $P_{(R,v)}u \odot P_{(R,u)}v$	SVD's (m, k)

Table 6: Comparison of composition operators that combine two word vector representations, $u, v \in \mathbb{R}^n$ and their learning parameters. Our model only needs two hyper-parameters: the number of prototype words m and dimensional reduction k in SVD