# Syntax-based decoding 

JHU Machine Translation class
April 1, 2014

## Administrative

- Homework 4 out, due April 14
- Final project proposals due today


## Where do grammars come from?

- We left off on Thursday with
-a formalism for describing the relationship between two languages,
-an loosely-sketched algorithm for producing translations
- Questions for today:
-Where do synchronous grammars come from?
-How do we decode with an ngram language model?


## Data－driven grammar extraction

－Grammar rules are not written by hand，they are extracted from bilingual parallel corpora

Arabic

| فالتعذيب لا يزال يمارس على نطاق واسع |
| :---: |
| وتتم عمليات الاعتقال والاحتجاز دون سبب بصورة روتينية |
| وحان وقت التحلى بالبصيرة والشجاعة السياسية ． |
|  |

## Chinese

我国 能源 原材料 工业 生产 大幅度 增长。

非国大 要求 阻止 更 多 被 拘留 人员 死亡。

English
Torture is still being practised on a wide scale．

Arrest and detention without cause take place routinely．
This is a time for vision and political courage

## English

China＇s energy and raw materials production up．
ANC calls for steps to prevent deaths in police custodv．

## Hiero

- Consider the redundancy in this phrase table

Spanish
English
la bruja verde the green witch
la bruja roja the red witch
la bruja azúl the blue witch

- What generalization is missing?


## Hiero

- Synchronous grammar rules
$X \rightarrow$ la bruja $X_{(1)}\| \|$ the $X_{(1)}$ witch
$X \rightarrow$ verde \|\| green
- As a tree


green


## Hiero-style SCFG rules

- Most common type of SCFG in SMT is Hiero which has rules w/one non-terminal symbol
- Not as nice as linguistically motivated rules, does not capture the reordering in Urdu


North relations Korea

## Hiero

- Consider the redundancy in this phrase table

| Spanish | English |
| :---: | :---: |
| la bruja verde | the green witch |
| la bruja roja | the red witch |
| la bruja azúl | the blue witch |

- What generalization is missing?
- Hiero abandons conventional English syntax
- Relies instead on evidence-based phrasal "subtractions"


## Extracting Hiero rules


$X \rightarrow$ 与 北 韩 有 邦交， have diplomatic relations with North Korea
$X \rightarrow$ 邦交，
diplomatic relations
$X \rightarrow$ 北 韩，
North Korea
$X \rightarrow$ 与 $X_{1}$ 有 $X_{2}$ ， have $X_{2}$ with $X_{1}$

## Decoding

- We now have a way to obtain a synchronous grammar
- Last week, we sketched the decoding algorithm, which was based on parsing
- Today, we'll cover it in more detail, and correct a crucial omission (ngram language models)


## Review (I)

- We've discussed how syntactic differences between languages motivated reordering as a preprocessing step

Ich werde Innen den Report aushaendigen, damit Sie den eventuell uebernehmen koennen.


Ich werde aushaendigen Ihnen den Report, damit Sie koennen uebernehmen den eventuell.

## Review (2)

- We've also discussed synchronous grammar rules, which describe the generation of sentences in pairs

|  | Urdu | English |
| :---: | :---: | :---: |
| $\mathrm{S} \rightarrow$ | $\mathrm{NP}(1) \mathrm{VP}(2)$ | $\mathrm{NP}(1) \mathrm{VP}(2)$ |
| $\mathrm{VP} \rightarrow$ | $\mathrm{PP}(1) \mathrm{VP}(2)$ | $\mathrm{VP}(2) \mathrm{PP}(1)$ |
| $\mathrm{VP} \rightarrow$ | $\mathrm{V}(1) \mathrm{AUX}(2)$ | $\mathrm{AUX}(2) \mathrm{V}(1)$ |
| $\mathrm{PP} \rightarrow$ | $\mathrm{NP}(1) \mathrm{P}(2)$ | $\mathrm{P}(2) \mathrm{NP}(1)$ |
| $\mathrm{NP} \rightarrow$ | hamd ansary | Hamid Ansari |
| $\mathrm{NP} \rightarrow$ | na\}b sdr | Vice President |
| $\mathrm{V} \rightarrow$ | namzd | nominated |
| $\mathrm{P} \rightarrow$ | kylye | for |
| $\mathrm{AUX} \rightarrow$ | taa | was |

## Review (3)

- ...and how we could extract those rules automatically from text


have $X_{3}$ with $X_{2}$

diplomatic North relations Korea


## Today

- How do we actually decode with these grammars?
- The solution is the CKY / CYK algorithm
- Outline

| \{CKY algorithm $\}$ | $\{$ CYK algorithm $\}$ |
| :---: | :---: |
| 6,090 | $\sim 13,700$ |

- Parsing in one language


## Google

- Parsing in two languages with inversion transduction grammar (ITG)
- Decoding as parsing with synchronous context-free grammars (SCFG) and integrated language models
- Time-permitting: advanced topics


# Review: monolingual parsing 

Using the CKY algorithm to find (the best) structure for a sentence given a grammar

## Formal definitions

- Formal languages are (possibly infinite) sets of strings that are generated by a grammar
- e.g., $\{a+\}$ is a language of all strings with one or more as
- Its grammar could be written as

$$
A \rightarrow A a
$$

$$
A \rightarrow a
$$

- We can view natural languages in this manner, too
- e.g., the English language is the set of word sequences that constitute valid English sentences
- We believe there to be a grammar that generates those sentences
- We don't know what it is, but we have some guesses and approximations


## Parsing

- Given a sentence and a grammar, how do we find Sts structure?
- We'll use the CKY alg 6 Pithm (Cocke-Kasami-Younger) $\bigwedge_{\text {Vp }}$
- Basic jea: build smal/item民 before largen ones


Fred Jones was worn out sentence

$$
S \rightarrow N P V P
$$

$$
\mathrm{VP} \rightarrow \text { VBN PRT }
$$

$$
\mathrm{PRT} \rightarrow \mathrm{RP}
$$

$$
\mathrm{VP} \rightarrow \mathrm{VBD} V P
$$

$$
N P \rightarrow N N P N N P
$$

NNP $\rightarrow$ Fred $\mid$ Jones
VBD $\rightarrow$ was
VBN $\rightarrow$ worn
RP $\rightarrow$ out

## Parsing with CKY



$$
\begin{aligned}
\mathrm{S} & \rightarrow \mathrm{NP} \text { VP } \\
\mathrm{VP} & \rightarrow \text { VBN PRT } \\
\mathrm{PRT} & \rightarrow \mathrm{RP} \\
\mathrm{VP} & \rightarrow \mathrm{VBD} \mathrm{VP} \\
\mathrm{NP} & \rightarrow \text { NNP NNP } \\
\text { NNP } & \rightarrow \text { Fred } \mid \text { Jones } \\
\text { VBD } & \rightarrow \text { was } \\
\text { VBN } & \rightarrow \text { worn } \\
\mathrm{RP} & \rightarrow \text { out }
\end{aligned}
$$

## Implementation details

- Dynamic programming maintains a chart of items
- Each cell item represents the dynamic programming state
-(NNP, I, I), (S, I,5)
- The chart is the collection of all items

```
struct item {
    // d.p. state
    string nt;
    int i, j;
    // backpointer
    float score;
    Rule* rule;
    item* rhs1,
        rhs2;
}
```

- The score resolves alternate ways of constructing an item
- We also store backpointers: the items and rule used to construct each item

a.k.a. "predecessor"

## CKY algorithm

input: words[1..N]
for i in 1..N
for each unary rule $X \rightarrow$ words[i] add (X,i,i) to the chart
for span in 1..N

```
for i in 1..(N-span)
    j = i + span
```

    for \(k\) in i..j
    for rule \(X \rightarrow Y\) Z
        if ( \(Y, i, k\) ) and ( \(Z, k, j)\)
        add (X,i,j) to the chart
    output: ( $\mathrm{S}, 1, \mathrm{~N}$ )

## Parsing with CKY



| I |  | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Fred | NNP |  |  |  |  |
| Jones | NP | NNP |  |  |  |
| was |  |  | VBD |  |  |
| worn |  |  |  | VBN |  |
| out | $S=$ | $-=-=\frac{\text { VP }}{}$ | VP | RP <br> PRT | 5 |
|  | Fred | Jones | was | worn | out |

## item

```
nt = "S";
i = 1, j = 5;
score = -42.5;
Rule = &rule("S -> NP VP")
rhs1 = &item(NP,1,2);
rhs2 = &item(VP, 3,5);
```


## Reconstructing the best parse

- We can reconstruct the best parse by following backpointers
nodes.append(item(S,1,N))
while nodes.size() > 0:
item = nodes.pop()
print item
nodes.append(item.rhsr)
nodes.append(item.rhsl)


## nodes



| Fred | NNP |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Jones | $N P$ | NNP |  |  |  |
| was | ! |  | VBD |  |  |
| worn | ' |  |  | VBN |  |
| out | S |  | $\rightarrow \mathrm{VP}$ | VP | $\begin{gathered} \text { RP } \\ \text { PRT } \end{gathered}$ |
|  | Fred | Jones | was | worn | out |

$$
\begin{aligned}
& S \rightarrow N P \operatorname{VP}(1,5) \\
& \text { NP } \rightarrow \text { NNP NNP }(1,2) \\
& \text { NNP } \rightarrow \text { Fred }(1,1) \\
& \text { NNP } \rightarrow \text { Jones }(2,2) \\
& \mathrm{VP} \rightarrow \mathrm{VBD} \operatorname{VP}(3,5) \\
& \text { VBD } \rightarrow \text { was }(3,3) \\
& \mathrm{VP} \rightarrow \mathrm{VBN} \text { PRT }(4,5) \\
& \text { VBN } \rightarrow \text { worn }(4,4) \\
& \text { PRT } \rightarrow \text { RP }(5,5) \\
& \text { RP } \rightarrow \text { out }(5,5)
\end{aligned}
$$

## Parsing with CKY



## Parsing as (weighted) deduction

- Deductive reasoning:
- axioms: statements that are true or false ("it is raining")
- inference rules: statements that are conditionally true ("If it is raining and I am outside, I'll get wet'')
- goals: statements that are licensed by combinations of axioms, inference rules, and other conclusions ("I am wet")



## Parsing as (weighted) deduction

- input: words w[I..N]
$\left.\begin{array}{|c|c|l|}\hline \text { Axioms } & \overline{\overline{X \rightarrow w[i]}} & \text { for all }(X \rightarrow w[i]) \\ \hline \text { Inference rules } & \frac{X \rightarrow w[i]}{(X, i, i)} & \\ \hline \text { Goal } & (B, i, j) & (C, j, k) A \rightarrow B C \\ \text { in bottom-up order } \\ \text { (smaller spans first) }\end{array}\right)$


## Complexity

- Complexity of parsing is $\mathrm{O}\left(\mathrm{Gn}^{3}\right)$
- G - number of (binarized) rules in the grammar
- n - length of the sentence
- All those rules were binary; what about longer rules?
- e.g.,

- We have to enumerate every split point!


## CKY algorithm

input: words[1..N]
for i in 1..N
for each unary rule $\mathrm{X} \rightarrow$ words[i]
add (X,i,i) to the chart
for span in $1 . . \mathrm{N}$
for i in 1..(N-span)

$$
j=i+\operatorname{span}
$$

$$
\text { for } k_{1} \text { in i..j-1 }
$$

$$
\text { for } k_{2} \text { in } k_{1} . . j
$$


i.........k।.....k2........j
for rule $\mathrm{X} \rightarrow \mathrm{W} \mathrm{Y}$ Z
if ( $W, i, k 1$ ) and ( $Y, k 1, k 2$ ) and ( $2, k 2, j)$ add (X,i,j) to the chart
output: ( $\mathrm{S}, 1, \mathrm{~N}$ )

## Binarization into Chomsky Normal Form

- In general, for a rule with k RHS items, complexity is $\mathrm{O}\left(\mathrm{n}^{\mathrm{k+1}}\right)$ (and cumbersome, since you have to explicitly add inner loops to enumerate them)
- Fortunately, we can binarize rules to make them all have a rank of 2

two split points: $\mathrm{O}\left(\mathrm{n}^{4}\right)$



## CKY algorithm

- In summary, monolingual parsing:
- finds the best structure
- works bottom-up, enumerating all spans, from small to large, building searching for applicable rules and building new chart items
- works with the binarized form of a grammars (easily unbinarized afterward) for a complexity of $\mathrm{O}\left(\mathrm{Gn}^{3}\right)$

- all grammars are binarizable


## Synchronous parsing

## Synchronous parsing

- We can extend CKY to parse two languages at once!
- Consider the following grammar:

$$
\begin{array}{ll}
A \rightarrow \text { fat, gordos } & \text { (lexical) } \\
A \rightarrow \text { thin, delgados } & \\
N \rightarrow \text { cats, gatos } & \\
V P \rightarrow \text { eat, comen } & \text { (inverted) } \\
N P \rightarrow A^{(1)} N^{(2)}, N^{(2)} \mathbf{A}^{(1)} & \text { (straight) }
\end{array}
$$

- and the following sentence pair:
fat cats eat / gatos gordos comen


## Synchronous parsing

- We now have to enumerate pairs of spans
- instead of (i,j)...
- ...we have (i,j) and ( $\mathrm{s}, \mathrm{t}$ )
- For each of the bilingual blocks, we attempt to match both straight and inverted rules


$$
\begin{aligned}
& \mathrm{A} \rightarrow \text { fat, gordos } \\
& \mathrm{N} \rightarrow \text { cats, gatos } \\
& \mathrm{VP} \rightarrow \text { eat, comen } \\
& \mathrm{VP} \rightarrow \text { eat, como } \\
& \mathrm{NP} \rightarrow \mathrm{~A}^{(1)} \mathrm{N}^{(2)}, \mathrm{N}^{(2)} \mathrm{A}^{(1)} \\
& \mathrm{S} \rightarrow \mathrm{NP}^{(1)} \mathrm{VP}^{(2)}, \mathrm{NP}^{(1)} \mathrm{VP}^{(2)}
\end{aligned}
$$



## Relation to monolingual parsing

-Why do we combine like this?

- Think about monolingual CKY: combine adjacent spans

- These pieces are adjacent in both languages; it's only when we consider them together that reordering comes into play
-Why can't we do this?
- It doesn't make sense!

-What about these?
- Possible, but complex

gap

rank > 2


## CKY for synchronous parsing

input: source[1..N], target[1..M] for $\operatorname{span}_{1}$ in $1 . . N$

```
for i in 1..(N-span1)
    j = i + span_
        for k in i..j
```

        for \(\operatorname{span}_{2}\) in 1...M
        for s in 1..(M-span2)
            \(t=s+\operatorname{span}_{2}\)
                for \(u\) in s..t
                    for rule \(X \rightarrow\) [Y Z]
                    if (Y,i,k,s,u) and
                (Z,k,j,u,v) then
                    add (X,i,j,s,t) to chart
    output: (S,1,N,1,M)

| comen |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |

if (Y,i,k,s,u) and ( $\mathrm{Z}, \mathrm{k}, \mathrm{j}, \mathrm{u}, \mathrm{v}$ ) then add (X,i,j,s,t) to chart

## Synchronous parsing

- Complexity: $\mathrm{O}\left(\mathrm{GN}^{3} \mathrm{M}^{3}\right) \approx \mathrm{O}\left(\mathrm{GN}^{6}\right)$
-Why?
- We have to enumerate all valid combinations of six variables
- This can be seen in the six nested loops of the algorithm

$$
A \rightarrow \text { fat, gordos }
$$

$$
N \rightarrow \text { cats, gatos }
$$

$$
\mathrm{VP} \rightarrow \text { eat, comen }
$$

$$
\text { VP } \rightarrow \text { eat, como }
$$

$$
N P \rightarrow \mathbf{A}^{(1)} \mathbf{N}^{(2)}, \mathbf{N}^{(2)} \mathbf{A}^{(1)}
$$

$$
\mathrm{S} \rightarrow \mathbf{N P}^{(I)} \mathrm{VP}^{(2)}, \mathbf{N P}^{(I)} \mathrm{VP}^{(2)}
$$

| comen | $(3,3,3, B)$ | $(3,3$, <br> $3,3)$ |  |
| :---: | :---: | :---: | :---: |
| gordos | $(1,1$, <br> $2,2)$ | $(1,2$, <br> $1,2)$ |  |
| gatos |  | $(2,2$, <br> $1,1)$ |  |
|  | fat | cats | eat |

## Visualization of $\mathrm{O}\left(\mathrm{GN}^{6}\right)$ complexity

input: source[1..N], target[1..M]
l for $\operatorname{span}_{1}$ in $1 . . \mathrm{N}$
2 for i in 1..(N-span $\left.{ }_{1}\right)$
$j=i+\operatorname{span}_{1}$
3 for $k$ in i..j
for $\operatorname{span}_{2}$ in $1 . . M$
for $s$ in 1..(M-span $)_{2}$
$t=s+\operatorname{span}_{2}$
6 for $u$ in s..t for rule $X \rightarrow[Y Z]$
if (Y,i,k,s,u) and ( $Z, k, j, u, v$ ) then
add (X,i,j,s,t) to chart
output: ( $\mathrm{S}, 1, \mathrm{~N}, 1, \mathrm{M}$ )

## Synchronous binarization

- In the above, we considered two nonterminals (per side)
- What if we want more (Zhang et al., 2006)?

$$
\begin{aligned}
& \mathrm{S} \rightarrow \mathrm{NP}^{(1)} \mathrm{VP}^{(2)} \mathrm{PP}^{(3)}, \mathrm{NP}^{(1)} \mathrm{PP}^{(3)} \mathrm{VP}^{(2)} \\
& \mathrm{NP} \rightarrow \text { Powell, Baoweier } \\
& \mathrm{VP} \rightarrow \text { held a meeting, juxing le huitan } \\
& \mathrm{PP} \rightarrow \text { with Sharon, yu Shalong }
\end{aligned}
$$

- Three nonterminals? No problem:
- More?


## Permutations

- The nonterminals in the right-hand side of a rule define a permutation between the languages
- we assume the source language nonterminals are in order (wlog)
- intermingled terminal symbols do not affect binarization ability
- Example:

$$
\mathrm{S} \rightarrow \quad \mathrm{NP}^{(1)} \mathrm{VP}^{(2)} \mathrm{PP}^{(3)}, \mathrm{NP}^{(1)} \mathrm{PP}^{(3)} \mathrm{VP}^{(2)}
$$

- permutation: | 32



## Synchronous binarization

- Bad news: synchronous grammars can't be binarized in the general case (Shapiro \& Stephens, I99I;Wu, 1997) *
- Famous examples: the $(2,4, I, 3)$ and $(3, I, 4,2)$ permutations

-What makes these unbinarizable?
- Crucial: parsing works by combining adjacent elements
- No pair of alignments here is adjacent in both languages simultaneously
(*) Technically, you can binarize any synchronous grammar, but you may increase the fan-out, which mitigates the potential gains.


## Synchronous binarization

- As the rank of a rule grows, the percentage of binarizable rules approaches 0
- In summary:

- We can't binarize all rules
- The first unbinarizable rule has rank 4


## Silver lining

- Empirically, we don't observe that many non-binarizable rules (Zhang et al., 2006):


Figure 6: The solid-line curve represents the distribution of all rules against permutation lengths. The dashed-line stairs indicate the percentage of non-binarizable rules in our initial rule set while the dotted-line denotes that percentage among all permutations.

- ...and we can safely throw out the ones we do find
- $99.7 \%$ of rules extracted were binarizable
- many not were due to alignment errors


## Decoding as parsing

## Synchronous decoding

- Enough parsing; what we care about is decoding
- Parsing is relevant, though, because we can view decoding as a task where we are doing synchronous parsing but we don't happen to know the target side text
- This works by parsing with a source-side projection of the synchronous grammar rules
- At the end, we can follow backpointers to discover the most probable target side


## Updated data structure

- Just like regular parsing, we combine items in pairs to produce new items over larger spans:


## $\underline{(A, I, I)(N, 2,2)}$ <br> (NP, I,2)

- However, we also have to maintain our guess of the target side

A $\rightarrow$ fat, gordos
$N \rightarrow$ cats, gatos
VP $\rightarrow$ eat, comen
VP $\rightarrow$ eat, como
$N P \rightarrow A^{(1)} N^{(2)}, N^{(2)} A^{(1)}$
$S \rightarrow \mathrm{NP}^{(1)} \mathrm{VP}{ }^{(2)}, \mathrm{NP}^{(1)} \mathrm{VP}{ }^{(2)}$

## Decoding

- Again, a bottom-up process


$$
\begin{array}{ll}
\mathrm{A} \rightarrow \text { fat, gordos } & 1.0 \\
\mathrm{~N} \rightarrow \text { cats, gatos } & 1.0 \\
\mathrm{VP} \rightarrow \text { eat, comen } & 0.1 \\
\mathrm{VP} \rightarrow \text { eat, como } & 0.9 \\
\mathrm{NP} \rightarrow \mathrm{~A}^{(1)} \mathrm{N}^{(2)}, \mathrm{N}^{(2)} \mathrm{A}^{(1)} & 1.0 \\
\mathrm{~S} \rightarrow \mathrm{NP}^{(1)} \mathrm{VP}^{(2)}, \mathrm{NP}^{(1)} \mathrm{VP}^{(2)} & 1.0
\end{array}
$$

## Legend

_- straight rule application
-- - - inverted rule application

## Getting the translation

- Follow the backpointers

$$
\begin{aligned}
& \text { - (S, l, 3) } \\
& \text { - (NP, I, 2) } \\
& \text { - }(\mathrm{N}, 2,2) \rightarrow \text { gatos } \\
& \text { - }(\mathrm{A}, \mathrm{l}, \mathrm{l}) \rightarrow \text { gordos }
\end{aligned}
$$

- (VP,3,3) $\rightarrow$ como
- translation: gatos gordos como
* cats fat Ips-eat



## What happened?

- We forgot the language model
- We're inventing the target side (which is what decoding does), so we need to incorporate it
- How?
- Stack-based decoding: we maintained the last word
- Integration was easy because hypotheses always extended to the right
- Here, hypotheses are merged either straight or inverted


## Language model integration

## phrase-based

$$
\begin{gathered}
\text { <s> I } \\
\text { OOO }
\end{gathered}+\underset{\substack{\text { tengo } \\
\rightarrow \mathrm{am}}}{ }=\begin{gathered}
\text { <s> I am } \\
\text { OOO }
\end{gathered}
$$

## synchronous grammars

$$
\begin{array}{cc}
\begin{array}{c}
\mathrm{A}(1, \mathrm{I}) \\
1.0
\end{array}+\begin{array}{c}
\mathrm{N}(2,2) \\
1.0
\end{array} & \mathrm{~A}(1, \mathrm{I}) \\
1.0
\end{array}+\begin{gathered}
\mathrm{N}(2,2) \\
1.0 \\
\mathrm{NP} \rightarrow \mathrm{~A}^{(1)} \mathrm{N}^{(2)}, \mathrm{N}^{(2)} \mathrm{A}^{(1)} \\
= \\
\mathrm{NP} \rightarrow \mathrm{~A}^{(1)} \\
\mathrm{N}(1,2) \\
1.0 \\
\text { (2) }, \mathrm{A}^{(1)} \\
\text { gatos gordos }
\end{gathered}
$$

## Language model integration

- We still maintain a chart of items, but now the items have to contain the target side words
- Just like regular parsing, we combine items in pairs to produce new items over larger spans
- When items are merged, we can use these words to compute a language model probability
- Formally, we are intersecting a context-free grammar (the translation model) with a regular grammar (Bar-Hillel et al., I964;Wu, I996)


## Updated data structure

- With dynamic programming, we only need a word on either side
- (for bigram LMs; for the general case, see Chiang (2007, §5.3.2))
- Following Chiang, we represent the elided middle portion with a $\star$
- The complete string can be reconstructed by following the backpointers

```
struct item {
    // d.p. state
    string nt;
    int i, j;
    string left_words;
    string right_words;
    // backpointer
    float score;
    Rule* rule;
    item* rhs1,
    rhs2;
}
```


## Decoding with an integrated LM



$$
\begin{array}{ll}
\mathrm{A} \rightarrow \text { fat, gordos } & 1.0 \\
\mathrm{~N} \rightarrow \text { cats, gatos } & 1.0 \\
\mathrm{VP} \rightarrow \text { eat, comen } & 0.1 \\
\mathrm{VP} \rightarrow \text { eat, como } & 0.9 \\
\mathrm{NP} \rightarrow \mathrm{~A}^{(1)} \mathrm{N}^{(2)}, \mathrm{N}^{(2)} \mathrm{A}^{(1)} & 1.0 \\
\mathrm{~S} \rightarrow \mathrm{NP}^{(1)} \mathrm{VP}^{(2)}, \mathrm{NP}^{(1)} \mathrm{VP}^{(2)} & 1.0 \\
& \\
& \\
& \\
& \\
\end{array}
$$

## Getting the translation

- Follow the backpointers
- (S, I , 3, gatos $\star$ comen)
- (NP, I, 2,gatos $\star$ gordos)
- (N,2,2,gatos) $\rightarrow$ gatos
- (A, I, I, gordos) $\rightarrow$ gordos
- $(\mathrm{VP}, 3,3$, comen $) \rightarrow$ comen
- translation:
gatos gordos comen
cats fat 3pp-eat



## Pruning

- We have also not dealt much with ambiguity and competition amongst hypotheses
- In general, there are too many hypotheses to consider, so we keep only the top $k$ of them (per input span (i,j))
- When considering a span (i,j) and a split point $k$, we have a large number of ways to combine items
- there can be any number of applicable rules
- there can be up to $k$ items located at span (i,k)
- there can be up to $k$ items located at span (k,j)


## Applying a unary rule

- The naive way is to consider the full cross product




## Cube pruning

- When considering a span ( $\mathrm{i}, \mathrm{j}$ ) of a length-N sentence:
- unary rules: there are rk items to compute ( $r$ the number of rules, $k$ the number of child items)
- binary rules: there are $\mathrm{Nrk}^{2}$ items to compute (since there are $\mathrm{O}(\mathrm{N})$ split points)
- However, we're only going to be keeping the top $k$ of them!
- this problem gets worse as $k$ gets larger
- We'd like to avoid computing all of these new items, which we accomplish with cube pruning


## Cube pruning

- We start with sorted lists of rules and the items they applied to
- Observation:
- the best item comes from the best rule and the best cell
- the next-best item uses either the $2 n d$ best rule or the 2nd-best cell

|  | rule | rhsl | rhsr |
| :---: | :---: | :---: | :---: |
| 1 | 1 | 1 | 1 |
| 2 | 2 | 7 | 3 |
| 3 | 4 | 9 | 4 |
| $\ldots$ |  |  |  |

best item

|  | rule | rhsl | rhsr |
| :---: | :---: | :---: | :---: |
| 1 | 1 | 1 | 1 |
| 2 | 2 | 7 | 3 |
| 3 | 4 | 9 | 4 |
| $\ldots$ |  |  |  |

2nd-best

|  | rule | rhsl | rhsr |
| :---: | :---: | :---: | :---: |
| 1 | 1 | 1 | 1 |
| 2 | 2 | 7 | 3 |
| 3 | 4 | 9 | 4 |
| $\ldots$ |  |  |  |

3rd-best

## Applying a unary rule

－The Huang \＆Chiang（2005）way：

| 등 | $\frac{\sqrt{\pi}}{2}$ | $\begin{aligned} & \tilde{\ddot{U}} \\ & \stackrel{0}{0} \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { 区 } \\ & \text { E } \\ & \text { U } \end{aligned}$ | $\frac{\text { 즐 }}{}$ | $\begin{aligned} & \tilde{U} \\ & \frac{0}{0} \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { © } \\ & \text { U } \\ & \text { U } \end{aligned}$ | $\frac{\pi}{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\pm$ | $\stackrel{1}{\square}$ | $\pm$ | $\pm$ | $\pm$ | $\cong$ | $\pm$ | $\pm$ |
|  | $\ddagger$ | $\ddagger$ | $\pm$ | \＃ | $\ddagger$ | $\pm$ | F |
| ${ }^{\infty}$ | － | ${ }_{0}^{\infty}$ | － | － | － | － | － |
| － | 㐅 | 㐅 | 㐅 | 㐅 | 㐅 | $\times$ | － |


|  | 14 |  | 147 |  |  | 147 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $X \rightarrow\left\langle\right.$ cong $X_{\text {过 }}$ ，from $\left.X_{\text {过 }}\right\rangle$ | 2.1 | 5.1 | 2.1 | 5.1 | 8.2 | 2.1 | 5.1 | 8.2 |
| $X \rightarrow\left\langle\right.$ cong $X_{\square \square}$, from the $\left.X_{\square}\right\rangle 2$ | 5.5 |  | 5.5 | 8.5 |  | 5.5 | 8.5 |  |
| $X \rightarrow\left\langle\right.$ cong $X_{\square \square}$ ，since $\left.X_{\square}\right\rangle$ ， 6 |  |  |  |  |  | 7.7 |  |  |
| $X \rightarrow\left\langle\operatorname{cong} X_{\square}\right.$ ，through $\left.X_{\square}\right\rangle 10$ |  |  |  |  |  |  |  |  |

## Cube pruning

- We haven't discussed the language model, which complicates this procedure by making it nonmonotonic
- But that's the basic idea


## Summary

- Today, we have reviewed
- Monolingual parsing
- Synchronous (bilingual) parsing
- Decoding as parsing with an intersected bigram language model
- We have also briefly touched on efficiency considerations with cube pruning


## Advanced topics

## Advanced topics: implicit binarization

- We'd decoded in an ITG settings, where the rules all look like this:

$$
\begin{array}{ll}
X \rightarrow \text { boy, chico } & \text { (lexical) } \\
X \rightarrow X^{(1)} X^{(2)}, X^{(2)} X^{(1)} & \text { (inverted) } \\
X \rightarrow X^{(1)} X^{(2)}, X^{(1)} X^{(2)} & \text { (straight) }
\end{array}
$$

- This is the closest thing to Chomsky Normal Form for synchronous grammars
- How do we decode with intermingled terminals and nonterminals?

$$
X \rightarrow \text { the } X^{(1)} \text { was } X^{(2)} \text {, el } X^{(1)} \text { era } X^{(2)}
$$

## Advanced topics: implicit binarization

- One answer: binarize (terminals can always be binarized):
$\mathbf{X} \rightarrow$ the $\mathbf{X}$ was $\mathbf{X}$, el $\mathbf{X}$ era $\mathbf{X}$
$X \rightarrow$ the $X_{174}$, el $X_{174}$


$$
\begin{aligned}
& X_{174} \rightarrow \mathbf{X} X_{295}, \mathbf{X} X_{295} \\
& X_{295} \rightarrow \text { was } \mathbf{X}, \text { era } \mathbf{X}
\end{aligned}
$$

- However, this is inefficient:
- it leads to a huge blowup in the number of nonterminals
- it introduces a split point that has to be searched over (avoidable in this case, but not always)


## Advanced topics: implicit binarization

- Instead, we'd like to do implicit, Earley-style binarization


## Advanced topics: spurious ambiguity

- Spurious ambiguity - multiple structures leading to the same interpretation
- Especially problematic in ITG with its weak grammar
- This can be addressed in various ways
- Grammar canonical forms

